

Model hierarchies for understanding atmospheric circulation

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Key Points:

- Model hierarchies help address open research questions. We focus on how they have improved our understanding of atmospheric circulation.
- Key benchmark models are identified that have helped to advance our understanding of the atmospheric circulation.
- The model hierarchies are commonly referred to but remain poorly defined. We identify three principles to organize models into hierarchies.

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Abstract

In this review, we highlight the complementary relationship between simple and complex models in addressing key scientific questions to describe Earth's atmospheric circulation. The systematic representation of models in steps, or hierarchies, connects our understanding from idealized systems to comprehensive models, and ultimately the observed atmosphere. We define three interconnected principles that can be used to characterize the model hierarchies of the atmosphere. We explore the rich diversity within the governing equations in *dynamical hierarchies*, the ability to isolate and understand atmospheric processes in *process hierarchies*, and the importance of choices in the physical domain and resolution in *hierarchies of scale*.

We center our discussion on the large scale circulation of the atmosphere and its interaction with clouds and convection, focusing on areas where simple models have had a significant impact. Our confidence in climate model projections of the future is embedded in our efforts to ground the climate predictions in fundamental physical understanding. This understanding is, in part, possible due to the hierarchies of idealized models that afford the simplicity required for understanding complex systems.

1 Introduction

In this review, we showcase idealized models which have enabled a deeper understanding of the large-scale circulation of the atmosphere and provide a set of principles for organizing them into hierarchies. We regard a *hierarchy* to be a sequence that connects our most simple models to our most complex, with the ultimate goal of explaining and predicting the behavior of Earth's atmosphere. The *simplicity*, or idealization, of a model is thus defined relative to other members of the hierarchy, where a simpler model seeks to reduce the problem to its most fundamental components at the cost of quantitative accuracy and realism.

We use simple models to ask fundamental science questions, which are ideally validated against observations of the real atmosphere. In practice, simple models are often validated against more complex models in the hierarchy. This is necessary when observations are sparse, such as in the upper stratosphere or Southern Hemisphere storm tracks, or not available, such as projecting future climates with different emission rates.

We are conscious of the subtle differences between a 'theory' and a 'model'. Here we consider a *model* to be a set of equations which seek to capture the behavior of the system in question, without necessarily regarding the model as representing the truth or having any general applicability. (A model is sometimes also taken to imply the *implementation* of an idea.) *Theory* may be regarded as the assumptions and, if needed, equations needed to economically describe or predict the behaviour of some phenomena or system. Still, the distinction is blurry, for a simple, testable model will have many of the attributes of a theory. Further, the behavior of a complex system may not be directly explainable by a simple theory in the conventional sense, and a model hierarchy itself then becomes a theory, or at least a hypothesis, for the system; some of these issues are discussed further in *Vallis* [2016]. In this review, we focus on models that may be deliberately simplified, and which implement a set of (usually time-dependent) equations in a more or less complex fashion, sometimes independently of any specific theory. Having differing degrees of complexity, connected to each other in some way, is the key step in sorting models into a hierarchy.

While the spectrum of available models has increased in the last decade or two, the idea of a 'hierarchy of climate models' in itself is not new. *Schneider and Dickinson* [1974] may have been the first to explicitly discuss the hierarchy in the sense we understand today, commenting that 'solid progress in understanding . . . climate change will require steady development of an almost continuous spectrum or hierarchy of models of increasing physical or mathematical complexity'. A decade later *Hoskins* [1983] noted the 'unhealthy' trend toward building models which are disconnected from one another and the real world, advocating, like *Schneider and Dickinson*, for a spectrum of connected models to provide a complete and balanced approach. *Nof* [2008] criticized the trend in climate modeling for higher resolution over increased understanding, and pointed out the danger of regarding

comprehensive models as ‘truth’. *Polvani et al.* [2017] noted that ‘Earth system models may be good for simulating the climate system but may not be as valuable for understanding it’.

This gap between our understanding of the atmospheric circulation and the increasing complexity of global circulation models was the focus of *Held* [2005] and *Held* [2014]. In these essays, *Held* echoed earlier concerns about relying too much on comprehensive models that we do not fully understand. He argued, however, that we should be equally concerned that our simpler models are capable of addressing our key scientific questions. He called for more study of ‘elegant’ models that are sufficiently complex to capture key elements of the real atmosphere, but still simple enough to provide understanding.

There is certainly no single unique hierarchy. Instead, a suitable model hierarchy may be constructed based on the key scientific questions of interest, as not all models are suitable for all purposes. Even for a given scientific problem different scientists will make different, perhaps equally defensible, choices. Nevertheless, we can attempt to produce a classification system to describe models as being simple or complex within the spectrum of available models. *Bony et al.* [2013] intuitively describe the complexity of climate models, see Figure 1a, as a balance between simplicity of the model and complexity of the system that is being modelled. More recently, *Jeevanjee et al.* [2017] describe the climate model hierarchy, see Figure 1b, in terms of dynamics, boundary layer forcing, and bulk forcing. In section 2 we propose an alternative, but complementary, description based on organizing the model hierarchies in terms of three principles.

In this discussion of the large-scale circulation of the atmosphere, we focus our review on the science questions that have been addressed using key idealized models. We structure our review to start with the most simple models and build up toward the more complicated models used to investigate the large-scale circulation within the mid-latitudes, middle atmosphere and tropics, Sections 3, 4 and 5, respectively. We then discuss the important role moisture plays in setting the atmospheric circulation in Section 6 and how the hierarchies have helped improve the representation of, and theory for, the Madden-Julian Oscillation in Section 7. We then summarize in Section 8.

We do not attempt to review all models. Instead, we describe a subset of simple models, discuss their broad use and then make connections from the simple models through to the coupled atmosphere-ocean General Circulation Models (GCMs). (The role of GCMs are discussed more in *Ghil and Robertson* [2000].) We will not discuss Earth System Models, the very complex models that include more processes than typical GCMs (e.g., biogeochemistry), but we do acknowledge that Earth System Models form an end point (if only by definition) in modelling processes that affect Earth’s climate and biogeochemistry.

2 Three principles guiding model hierarchies

There is no single or ubiquitous model hierarchy for the atmosphere. Many model hierarchies are possible, depending in part on the science questions to be addressed. Nevertheless, a broad classification of the hierarchies is useful and here we define three principles that can be used to guide the categorization of the model hierarchies.

The first principle is the *dynamical* hierarchies of the atmospheric fluid flow. The dynamical hierarchies allow us to isolate and explore the importance of different temporal and spatial scales on the governing equations.

The second principle is the *process* hierarchies of the atmosphere. The process hierarchies allow for the stepwise integration of important atmospheric processes into the governing equations of the fluid flow. We systematically advance terms with the thermodynamic equation to form a sequence of models that make a smaller ‘diabatic hierarchy’. An additional aspect of the process hierarchies are the boundary conditions, such as surface properties such as aquaplanets, topography or orography.

The third principle is the *hierarchies of scale*, implicit to both the dynamical and process hierarchies, where the choice of physical domain and numerical resolution allows for the systematic

120 exploration of different dynamical and physical processes across all time and spacial scales. There
 121 are practical trade offs between scale and complexity due to the computation expense. Perhaps unlike
 122 the first two, this is not so much a hierarchy of complexity, but it does describe the practical decisions
 123 about space and time scales which are required when building a model.

124 Almost all theory and modeling efforts can be classified into a hierarchy of some form, so
 125 attempting to catalogue *all* the hierarchies is not helpful. In the remainder of this paper, we
 126 selectively highlight examples of model hierarchies, specifically those that include simple models
 127 and that have advanced our understanding of the large scale circulation of the atmosphere. We focus
 128 on these models not because they necessarily optimally cover the complexity of available models, but
 129 rather because they have been extensively studied, thus establishing their impact. In the remainder of
 130 this review we incrementally build upon the different aspects of the process hierarchy, starting with
 131 the circulation within the mid-latitudes.

132 **3 The Mid-Latitude Circulation**

133 The large-scale extratropical circulation provides one of the best success stories for hierarchical
 134 climate modeling: some key aspects of the underlying dynamics are now reasonably well understood
 135 and part of modern textbooks [e.g. Vallis, 2017]. Other aspects are still areas of active research,
 136 such as the non-linear dynamics related to eddy-mean flow interaction. Idealized simulations have
 137 played an instrumental role in this progress, providing key insights on the non-linear behavior
 138 of extratropical disturbances. Since the early days of climate modeling, theorists recognized the
 139 great power of numerical computing as a means to overcome the stringent limitations of analytical
 140 work. Idealized simulations aimed at understanding the atmosphere were performed in parallel with
 141 comprehensive simulations. Some of the insight gained with these early simulations constitute the
 142 basis of prevalent paradigms on the extratropical circulation.

143 We begin by highlighting two models that have allowed us to isolate the key elements of the mid-
 144 latitude circulation. The first is a class of *barotropic vorticity equation models*, where collapsing the
 145 vertical dimension allow us to focus on feedbacks between the zonal mean flow, Rossby waves, and
 146 the spherical geometry of the planet. The second is the *two-layer quasi-geostrophic (QG) channel*
 147 *model*, which provides perhaps the most simple context for understanding baroclinic instability. We
 148 then discuss an idealized approach to combining elements of the baroclinic and barotropic dynamics
 149 together in eddy life cycle experiments.

150 **3.1 Rossby-wave dynamics: The barotropic vorticity equations on the sphere**

151 Rossby-wave propagation plays a fundamental role in both upper-troposphere synoptic vari-
 152 ability and the remote atmospheric response to forcing. The barotropic model provides a simple
 153 framework for studying these processes. In addition to providing the first numerical weather simu-
 154 lations [Charney *et al.*, 1950], the barotropic model served as a test bed to understand the influence
 155 of topography and localized heating on the general circulation [Grose and Hoskins, 1979; Hoskins
 156 and Karoly, 1981]. These experiments revealed the important role played by the mean flow structure
 157 for Rossby wave refraction in the upper troposphere. The widely used concepts of waveguides and
 158 propagation windows are based on these ideas, which are key to our understanding of the extratropical
 159 response to El Niño.

160 So-called ‘stirred’ barotropic models [e.g., Vallis *et al.*, 2004] have seen a resurgence in recent
 161 years for understanding upper-troposphere synoptic variability and the dynamics of eddy momentum
 162 fluxes and eddy-driven jets without the complexity of baroclinic dynamics. In this model, the impact
 163 of baroclinic instability is approximated by a prescribed forcing (the stirring) in the vorticity equation
 164 at the synoptic scales. As a result, there are explicitly no feedbacks of the barotropic circulation
 165 on eddy generation. The model has been used as a conceptual model of annular mode variability
 166 to explain the dependence of zonal index persistence on latitude [Barnes *et al.*, 2010] and to study
 167 the interaction between the tropical and subtropical jets [O’Rourke and Vallis, 2013], among other
 168 problems.

As a further simplification, when the model is linearized it is possible to obtain a set of closed solutions (for simple forms of stirring) using stochastic theory [DelSole, 2001]. Lorenz [2014] has devised a very sophisticated method to calculate the eddy momentum flux given the full space-time characteristics of the stirring, which can play an important role due to the impact of wave phase speeds on refraction indices and wave propagation [Barnes and Hartmann, 2011]. The barotropic model can be a useful tool for exploring ‘eddy-momentum-flux closures’, i.e., the sensitivity of the direction of wave propagation to the mean state and/or model configuration. This remains a challenging open question in general circulation theory.

3.2 Baroclinic instability: The two-layer quasi-geostrophic model

To capture the essence of the eddy generation process, the *two-layer quasi-geostrophic model on the f -plane* stands out as a benchmark, indeed classical, model of the extratropical baroclinic circulation [Phillips, 1956]. It vies with the Eady model [Eady, 1949] as the simplest model that can produce baroclinic instability in a fashion relevant to the real world. There is only one baroclinic mode and the stratification and radius of deformation are prescribed.

The model also provides a simplified framework for studying the nonlinear extratropical circulation in a forced-dissipative configuration, in which the flow is typically forced by thermal relaxation to a baroclinic jet and the lower layer wind is damped using Rayleigh friction [e.g. Zurita-Gotor, 2007]. The f -plane approximation and constant deformation radius make upper-troposphere dynamics simpler than in the spherical case (the symmetry of the model makes northward and southward propagation equally likely). In this sense, the model is complementary to the barotropic model in that it is devoid of the barotropic feedbacks associated with sphericity that play an important role in the dynamics of that model. The two-layer model not only reproduces qualitatively the main features of the observed extratropical circulation but it also captures more subtle aspects of extratropical dynamics like the clustering of eddies in wavepackets [Lee and Held, 1993], the driving of low-frequency baroclinicity variability [Zurita-Gotor et al., 2014] or the character of lower-troposphere eddy momentum fluxes [Lutsko et al., 2017].

In its forced configuration, the two-layer model provides the lower end of a dynamical hierarchy of forced-dissipative dry models, in which the mean climate is determined by the competition between the eddy fluxes and very idealized forms of forcing. These models can be formulated at different levels of complexity along the dynamical hierarchy depending on the scientific problem of interest [e.g. Zurita-Gotor and Vallis, 2009; Lachmy and Harnik, 2014; Jansen and Ferrari, 2013].

At the high end of this dynamical hierarchy, the model of Held and Suarez [1994] has been widely used to study various aspects of the extratropical circulation and its sensitivity to climate change [e.g. Lorenz and DeWeaver, 2007; Butler et al., 2010; Yuval and Kaspi, 2016] due to its realistic circulation. This model uses a primitive-equation formulation and a spherical domain and is forced by relaxation towards a state approximating radiative convective equilibrium (described in Section 6.1), with near moist-neutral stratification in the vertical but strong meridional temperature gradients. Above the tropopause, the atmosphere is simply relaxed towards an isothermal state. A variant of this model better suited for the tropical circulation combines relaxation to pure radiative-equilibrium with an idealized convection scheme designed to mimic the stabilizing effect of latent heating by moist convection [Schneider and Walker, 2006].

3.3 Connecting eddy growth, propagation, and decay: The eddy life-cycle paradigm

Even in the very idealized physical setting described above, the time-dependent evolution of forced-dissipative models is inherently nonlinear and turbulent. As a key simplification to the full non-linear problem, the series of experiments systematized by Hoskins and collaborators in the 1970’s, building on pioneering numerical work by Edelmann [1963] and others, provided insight on the nonlinear evolution of baroclinic modes. The analysis of an eddy lifecycle by Simmons and Hoskins [1978] introduced the notions of baroclinic growth and barotropic decay as an idealized conceptual model for the nonlinear evolution of extratropical disturbances. Similar ideas, but in the

218 more general context of a statistical steady state and using quasi-geostrophic theory to interpret the
 219 simulations, were introduced independently by *Salmon* [1980]. This simple paradigm has survived
 220 to today and plays a fundamental role for our understanding of wave–mean-flow interaction and the
 221 maintenance of the mean circulation. Additional analysis [*Simmons and Hoskins*, 1980] uncovered
 222 the sensitivity of the decay stage in the lifecycle to the mean state, identifying two distinct patterns
 223 of evolution.

224 As theoretical advancements clarified the relation between eddy propagation and wave-mean
 225 flow interaction [*Andrews and McIntyre*, 1978; *Edmon et al.*, 1980] and the focus on Potential Vorticity
 226 (PV) dynamics highlighted the important role of wave breaking [*McIntyre and Palmer*, 1983],
 227 *Thorncroft et al.* [1993] proposed a conceptual model for understanding the two idealized lifecycles
 228 based on the direction of propagation and the typology of wave breaking. Idealized simulations
 229 were also useful for demonstrating the relevance of critical layer theory for eddy dissipation and
 230 wave-mean flow interaction in eddy lifecycles [*Feldstein and Held*, 1989]. The critical layer is a
 231 powerful concept for constraining upper-troposphere propagation [*Randel and Held*, 1991] and plays
 232 an important role for extratropical variability and climate sensitivity [*Lee et al.*, 2007; *Chen and*
 233 *Held*, 2007; *Ceppi et al.*, 2013].

234 The association between the direction of propagation, the topology of wave breaking and the
 235 sign of the eddy momentum flux uncovered by the idealized studies is central to our understanding
 236 of jet shifts and phenomena like the North Atlantic Oscillation [*Rivière and Orlanski*, 2007]. On the
 237 sphere, equatorward propagation and poleward momentum fluxes dominate [*Thorncroft et al.*, 1993;
 238 *Balasubramanian and Garner*, 1997] so that we might expect extratropical jets to shift poleward
 239 as they strengthen if the stirring does not move. However, idealized studies show that the direction
 240 of propagation is affected by many other factors, such as the latitude and scale of the eddies,
 241 the barotropic shear and the low-level baroclinicity [*Simmons and Hoskins*, 1980; *Hartmann and*
 242 *Zuercher*, 1998; *Rivière*, 2009], among others. Due to this complexity, we are still far from a complete
 243 theory for the eddy momentum flux closure.

244 **3.4 Case Study: Eddy feedbacks and the variability of the jet stream**

245 To illustrate the use of hierarchical modeling in the extratropics, we discuss its application to
 246 the analysis of eddy feedbacks in unforced jet variability. We have chosen this example because it
 247 lends itself well to the hierarchical approach and because it is a topic of current research.

248 The leading (and more persistent) mode of extratropical zonal wind variability consists of a
 249 meridional shift of the eddy-driven jet concomitant with annular mode variability [*Thompson and*
 250 *Wallace*, 2000]. *Lorenz and Hartmann* [2001] found a positive correlation between the jet anomalies
 251 and their eddy momentum driving in the Southern Hemisphere when the jet leads by a few days,
 252 see Figure 2a, which implies that the anomalous eddy momentum fluxes tend to extend the duration
 253 of the jet anomalies. They interpreted this positive correlation as depicting the sensitivity of the
 254 anomalous eddy momentum flux on the state of the jet, or a positive eddy feedback (but see *Byrne*
 255 *et al.* [2016] for an alternative interpretation).

256 Climate models are known to be too persistent [*Gerber et al.*, 2008], see Figure 2b, particularly
 257 idealized models [*Gerber and Vallis*, 2007]. This is mostly associated with too slow decay of the
 258 autocorrelation function at lags beyond 5 days, see Figure 2c, suggesting an excessive eddy feedback.
 259 Two different types of mechanisms have been proposed in the literature for this feedback: barotropic
 260 and baroclinic. Barotropic mechanisms rely on changes in upper-troposphere propagation due to
 261 changes in refraction in the presence of the anomalous jet, which may involve a number of different
 262 mechanisms [*Lorenz*, 2014; *Burrows et al.*, 2017]. In contrast, baroclinic mechanisms attribute the
 263 eddy momentum flux changes to changes in the stirring driven by the changes in the barotropic flow
 264 [*Robinson*, 2000].

265 Idealized models provide a useful framework for studying these two aspects of the problem in
 266 isolation. Using the stirred barotropic model, *Barnes et al.* [2010] investigated the sensitivity of the
 267 eddy momentum fluxes to the anomalous jet with fixed stirring. They showed that on the sphere, the

268 eddy momentum flux becomes more asymmetric (equatorward propagation is enhanced) when the
 269 jet moves poleward, leading to a positive feedback. This may be understood in terms of changes in
 270 the turning latitude/reflecting level [Lorenz, 2014].

271 In the opposite direction, Zurita-Gotor *et al.* [2014] analyzed the dynamics of jet variability
 272 in idealized two-layer QG simulations and showed that the enhanced persistence in that model
 273 was consistent with the baroclinic feedback mechanism of Robinson [2000]. They found evidence
 274 of baroclinicity driving the barotropic flow and very large coherence between the eddy heat and
 275 momentum fluxes at low frequency, with the momentum fluxes leading the variability, see Fig 2e.
 276 The co-variability between the barotropic and baroclinic components of the wind is also a robust
 277 result in observations [Blanco-Fuentes and Zurita-Gotor, 2011] and comprehensive climate models.
 278 In Figure 2d the large correlation between the long-lag decay rates of (barotropic) jet anomalies
 279 and baroclinicity is shown for a selection of CMIP5 models, so that models with more persistent jet
 280 variability also tend to have more persistent baroclinicity.

281 Stirred barotropic models can capture some aspects of the observed jet variability, like the sen-
 282 sitivity of persistence to latitude [Barnes *et al.*, 2010]. On the other hand, the baroclinic mechanism
 283 may help explain the excessive persistence bias in comprehensive climate models (which cannot
 284 be corrected by eliminating the jet latitude bias; Simpson *et al.* [2013]) or in idealized baroclinic
 285 models. Finally, diabatic effects may also play a role for annular mode persistence [Xia and Chang,
 286 2014]. The jet persistence problem underscores the importance of making connections across the
 287 full model hierarchy, as the mechanisms at work may not be the same in all steps of the hierarchy, in
 288 comprehensive climate models and in the real atmosphere.

289 4 The Middle Atmosphere Circulation

290 Work over the last two decades has established the highly coupled nature of the circulation in the
 291 troposphere and stratosphere. Many comprehensive atmospheric models now treat the stratosphere-
 292 troposphere as one system [e.g. Gerber *et al.*, 2012], recognizing the consequences of underresolving
 293 the middle atmosphere for weather and climate prediction [e.g., Sigmond *et al.*, 2013; Manzini
 294 *et al.*, 2014]. Historically, however, the middle atmospheric research proceeded on a different track
 295 after Charney and Drazin [1961] showed that a detailed representation of the stratosphere was not
 296 necessary to capture the basic structure of synoptic variability in the troposphere.

297 Wave-mean flow theory was developed, in part, to explain and understand the stratospheric
 298 circulation. The gross structure of the stratosphere can not be explained without understanding the
 299 essential role of waves in the transport of momentum, mass, and tracers. We highlight three models
 300 that capture these interactions, and the more sophisticated steps in the hierarchy they have inspired.

301 4.1 Sudden Stratospheric Warming Events: The Holton and Mass [1976] Model

302 Cooling during the polar night generates a strong westerly jet in the winter stratosphere, often
 303 referred to as the stratospheric polar vortex, where wind speeds can sometimes reach 100 ms^{-1} . In
 304 the early 1950s, however, it was observed that the polar vortex in the boreal hemisphere aperiodically
 305 undergoes a rapid breakdown. The reversal of the westerly winds is associated with a dramatic
 306 warming (40 K or more in the course of a few days) and hence known as a Sudden Stratospheric
 307 Warming (SSW) [Scherhag, 1952]. SSWs occur on average once every other year in the Northern
 308 Hemisphere, but only one such event (in 2002) has been observed in the austral hemisphere. Baldwin
 309 and Dunkerton [2001] showed that SSWs affect the troposphere, shifting the jet stream equatorward
 310 with substantial impacts on weather in Europe and Eastern North America. The tropospheric impact
 311 persists on the 1-2 month time scale that it takes the stratospheric vortex to recover back to its
 312 climatological state.

313 Matsuno [1971] proposed a dynamical mechanism for SSWs based on planetary scale wave
 314 propagation from the troposphere. Long before this process could be captured in atmospheric
 315 GCMs, Holton and Mass [1976] developed a simple, stratosphere-only, model that captures the

316 essence of these abrupt events. They constructed a highly truncated baroclinic quasi-geostrophic
 317 model, retaining only wavenumber 1 and the mean flow. The mean state is forced by Newtonian
 318 relaxation toward a specified state of radiative equilibrium, the wave generated by specifying a forcing
 319 amplitude on the bottom boundary. The model exhibits an abrupt transition between subcritical and
 320 supercritical behavior depending on the amplitude of the wave forcing: in the subcritical state,
 321 westerly winds coexist with a stationary Rossby wave. If the wave amplitude at the lower boundary
 322 exceeds a critical threshold, however, the model transitions abruptly to a new equilibrium: the waves
 323 grow, weakening the westerlies until they reverse, i.e., a prototypical SSW.

324 Multiple flow equilibria have also been demonstrated in more complex 3-dimensional stratosphere-
 325 only models – again forced by specifying the amplitude of planetary waves at the lower boundary
 326 – but permitting arbitrary height and latitude structure above [e.g., *Scott and Haynes*, 2000; *Scott*
 327 *and Polvani*, 2006]. The highly idealized *Holton and Mass* [1976] model, however, has continued to
 328 inspire research on the role of gravity waves in SSWs [e.g., *Albers and Birner*, 2014], and the role
 329 of the stratosphere on regulating wave activity [e.g., *Sjoberg and Birner*, 2014].

330 These models suggest that the near absence of SSWs in the austral hemisphere is due to the
 331 fact that stationary wave amplitude is weaker, a process explored in full 3-D atmospheric models
 332 using a *Held and Suarez* [1994] forcing, albeit with a modified equilibrium temperature profile in
 333 the stratosphere to establish a polar vortex. *Taguchi et al.* [2001], *Taguchi and Yoden* [2002], and
 334 *Sheshadri et al.* [2015] show how one can transition from a Southern Hemispheric state to a Northern
 335 Hemispheric state by increasing the amplitude of surface topography. *Held and Suarez* [1994] type
 336 models have also allowed for exploration of the impact of the vortex strength on the troposphere, both
 337 in response to forced changes [*Polvani and Kushner*, 2002] or SSWs [*Gerber and Polvani*, 2009].

338 **4.2 The Quasi-Biennial Oscillation: A physical model**

339 While high latitude variability in the stratosphere is dominated by interactions between planetary
 340 scale waves and the mean flow, tropical variability is effected by wave-mean flow interactions
 341 involving much smaller-scale gravity waves. The Quasi-Biennial Oscillation (QBO) is an oscillation
 342 of the zonal mean wind in the tropical stratosphere with a period of approximately 28 months,
 343 associated with the slow downward migration of alternative westerly and easterly jets [see *Baldwin*
 344 *et al.*, 2001, for a comprehensive review]. The long time scales of the QBO make it a potential
 345 source of predictability in the troposphere. For example, it was recently observed that the QBO is
 346 associated with changes in the strength and predictability of the Madden-Julian Oscillation [e.g., *Yoo*
 347 *and Son*, 2016]. The QBO also provides another example of the advances that a simplified system
 348 can bring about, well ahead of our ability to simulate the phenomenon in comprehensive models.

349 Pioneering work by *Lindzen and Holton* [1968] and *Holton and Lindzen* [1972] proposed that
 350 the QBO could be explained as an interaction between gravity waves and the mean flow. Selective
 351 absorption (breaking) of waves carrying easterly (westerly) momentum on the lower flank of easterly
 352 (westerly) jets leads to a momentum tendency that pulls the jet downward, enough to oppose the
 353 tendency of the mean tropical upwelling to advect the jet upward. The balance between the two
 354 effects leads to the slow, 28 month period of the jets. These models came long before we had the
 355 ability to observe (or simulate) the small scale gravity waves implicated in the mechanism. Even
 356 today, gravity waves provide a challenge to observe and model [*Alexander et al.*, 2010].

357 Given the challenges associated with observing or directly simulating the processes involved in
 358 the mechanism, *Plumb and McEwan* [1978] developed a novel physical model of the phenomenon.
 359 Models of the atmosphere generally refer to numerical models, but *Plumb and McEwan* [1978] is
 360 a rare example of an experiment using a physical model. The *Plumb and McEwan* [1978] model
 361 consists of an annulus of stratified salt water and internal waves forced by mechanically oscillating
 362 the lower boundary. The waves generate spontaneous formation of jets (an azimuthal circulation in
 363 the annulus), with slow oscillations and reversal of the flow, similarly to the QBO of the atmosphere.

364 **4.3 Stratospheric transport: The leaky pipe**

365 Transport and chemistry play key roles in the distribution of trace gases throughout the strato-
 366 sphere, including water vapor, ozone, and the substances that deplete ozone. The meridional over-
 367 turning circulation of the stratosphere, known as the Brewer-Dobson Circulation, was first inferred
 368 from trace gas measurements, decades before we could observe the circulation directly [*Brewer,*
 369 *1949; Dobson, 1956*]. Trace gases are advected by the mean Lagrangian circulation of mass and
 370 mixed along isentropic surfaces in the process of wave breaking. The latter mixing process pro-
 371 duces no net transport of mass, but will transport a trace gas if there is a horizontal gradient in its
 372 concentration.

373 Efforts to understand stratospheric transport began with limiting cases in the balance between
 374 transport of tracers across isentropic surfaces by the mean overturning mass circulation vs. the mixing
 375 of tracers along isentropic surfaces. *Plumb and Ko* [1992] consider a circulation where mixing along
 376 isentropic surfaces is extremely efficient. In contrast, *Plumb* [1996] developed the idea of a ‘tropical
 377 pipe’, where upwelling air in the tropics is entirely isolated from the downwelling air in the higher
 378 latitudes and transport is set by the mean mass circulation alone. These two limiting cases were
 379 combined in a benchmark model in our understanding of transport processes, the ‘leaky pipe’ model
 380 of *Neu and Plumb* [1999].

381 The leaky pipe divides the stratosphere into two regions, an upwelling ‘pipe’ in the tropics, and
 382 a downwelling pipe in the extratropics of both hemispheres. Mass is advected up the tropical pipe
 383 by the Lagrangian mean circulation, detraining continually out to the extratropics. The boundary
 384 between the two regions, the edge of the stratospheric surf zone, is a barrier to transport, but the
 385 ‘leaky’ pipe allows for some mixing of mass between the two. The most important parameters are
 386 the net detrainment (or equivalently, the net Lagrangian transport) and total mixing as a function of
 387 height, and can be solved for analytically with appropriate simplifying assumptions. A key result of
 388 the model is that an increase in the net Lagrangian mass transport will tend to freshen the stratosphere,
 389 cycling tracers more quickly through it, while an increase in mixing tends to slow the cycling, as
 390 mixing leads to recirculation of air through the stratosphere.

391 While designed primarily as a conceptual model, the leaky pipe has been applied in a more
 392 realistic context to understand the make up of the stratosphere, and its response to anthropogenic
 393 forcing. *Garny et al.* [2014] use it to interpret changes in the stratospheric circulation in comprehen-
 394 sive models, separating the roles of mixing from the mean Brewer-Dobson Circulation. *Ray et al.*
 395 [2010] build on the leaky pipe to explain the distribution of trace gases, and *Linz et al.* [2016, 2017]
 396 use it to quantify the strength of the Brewer-Dobson Circulation from satellite measurements.

397 **5 The Large Scale Circulation of the Tropics**

398 Significant progress in understanding the large-scale circulation of the mid-latitudes and middle
 399 atmosphere was possible in the context of “dry dynamics”. Removing the non-linearities associated
 400 with moist processes simplifies the problem, both conceptually and in terms of the numerical
 401 equations, processes, and scales that must be represented or parametrized. Indeed, all the simple
 402 models highlighted in Sections 3 and 4 do not include moist effects. In the tropics, the circulation and
 403 moist processes are more intimately coupled. A key scientific challenge for understanding tropical
 404 circulation has been: How do we deconvolve the tight coupling between circulation, moisture, clouds,
 405 and convection?

406 Nonetheless, there are still “dry” frameworks for understanding the gross features of the tropical
 407 circulation. In Section 5.1 we explore the Matsuno-Gill model, a model that captures the equatorial
 408 zonal overturning circulation, or Walker circulation, using the dry shallow water equations. In
 409 Section 5.2 we then focus on the zonal mean tropical overturning circulation, the Hadley circulation,
 410 again starting the discussion with a dry atmospheric model, but quickly introducing an idealized
 411 GCM that begins to capture moist processes.

5.1 The Walker Circulation: The Matsuno-Gill model

The Walker circulation describes equatorial atmospheric cells with ascent over the Maritime Continent (equatorial Western Pacific) and descent in the Eastern Pacific or Indian Oceans. The number of equatorial circulation cells and the location of ascending/descending branches are coupled with SSTs and the phase of ENSO [Julian and Chervin, 1978]. Research questions for the Walker cell include: How does convection and circulation interact within the Walker circulation? How does the Walker circulation and El-Niño Southern Oscillation influence the onset of the monsoon? How will the Walker circulation change with global warming?

Similarly to the mid-latitudes, many simple models for the tropical circulation hinge on reducing the dimensions of the atmospheric flow and a key simplification is to vertically truncate the fluid governing equations. One such model that has been fundamental for understanding the structure of the Walker circulation is the Matsuno–Gill model [Matsuno, 1966; Gill, 1980], that uses the dry shallow water equations on an equatorial-beta plane with a stationary heating source [e.g. Vallis, 2017, section 8.5]. This single-layer model provides an analytic solution for the horizontal structure associated with the first baroclinic mode. This vertical mode captures the circulation driven by heating associated with tropical deep convection, and is characterized by opposite signed flow in the upper vs. lower troposphere. As the troposphere does not have a rigid upper boundary, it is not a true "mode" as in the ocean, but it often behaves like one.

The model's solution is generally described as the Matsuno–Gill pattern, in which two steady-state circulation cells develop in response to the applied heating, with low-level convergence into and upper-level divergence out of the heating region. This generates eastward propagating Kelvin waves and westward propagating Rossby waves. Two off-equatorial low pressure systems form as Rossby waves can not propagate along the equator [see Figure 8.11 of Vallis, 2017]. This equatorially-symmetric component of the Matsuno-Gill model generally describes the observed structure of the Walker circulation, with analogous tropical convection in the West Pacific and descent over the cold SST in the East Pacific (due to deep water upwelling).

The Matsuno–Gill model has also been used as the atmospheric component of the first successful numerical ENSO prediction model, the Cane-Zebiak model [Cane *et al.*, 1986]. a very influential reduced complexity coupled atmosphere-ocean model. In addition, the Matsuno-Gill model captures monsoonal circulations, using off-equatorial heating to mimic the seasonal cycle. Gill [1980] showed that the anti-symmetric Matsuno-Gill pattern (see Figure 3 of Gill [1980]), describes the general structure of the monsoon flow [Rodwell and Hoskins, 1996]. Furthermore, the Matsuno–Gill model is important for understanding the propagation of the Madden-Julian Oscillation, as detailed in Section 7.

While some aspects of the Walker circulation are captured by the Matsuno–Gill model, there are still many limitations. The primary limitation of the Matsuno-Gill model is that it does not interactively include moisture and, as a result, many important moist feedback mechanisms are absent. One approach to studying the moist Walker circulation is to impose a large-scale gradient of SST in a two-dimensional atmospheric model domain, creating a steady-state Walker circulation, commonly called the "mock" Walker circulation.

Bretherton *et al.* [2006] studied the moist Walker circulation using an idealized non-rotating 2D model, that is vertically truncated (one vertical moisture mode) following the approach of the quasi-equilibrium tropical circulation model [Neelin and Zeng, 2000], which assumes the weak temperature gradient (discussed more in Section 6.1), and has simple precipitation and cloud schemes; see their Figure 4 for the resulting circulation. This is a useful prototype model configuration because it allows explicit cloud resolving model (CRM) and GCM-physics comparisons of a climate relevant problem [Jeevanjee *et al.*, 2017]. The beauty of this idealized model is that it includes feedbacks between convection and the large-scale circulation. In comparing to 3D CRMs, Bretherton *et al.* [2006] showed many interesting features within the two models: similar precipitation but different humidity distributions, narrowing of the circulation with warming SSTs and the importance of moist

462 static energy in understanding feedbacks between convection and the large-scale circulation within
463 the Walker circulation.

464 **5.2 The Hadley Circulation: Gray Radiation Aquaplanets**

465 The Hadley circulation describes the zonally averaged atmospheric circulation cell with net
466 ascent near the equator, poleward outflow in the upper troposphere, descent in the subtropics, and
467 an equatorward near-surface return flow. The Hadley circulation separates the moist tropical regions
468 from the dry subtropical climate zones and as such is important for setting the surface climate. Key
469 research questions for the Hadley cell include: What controls its strength? What controls the position
470 of the descending branch (i.e., the tropical edge) and the near-equatorial ascending region? How will
471 these components change with global warming?

472 Dry models of the atmosphere have been illuminating in studying some of these research ques-
473 tions. The dry models used to investigate the dynamics of the Hadley cell range from axisymmetric
474 models amenable to theoretical progress [*Held and Hou*, 1980; *Lindzen and Hou*, 1988] through to
475 idealized dry GCMs with extratropical eddies that interact with the tropical circulation [*Kim and Lee*,
476 2001; *Walker and Schneider*, 2006]. The behavior across this dry model hierarchy has revealed two
477 important insights. First, that the Hadley circulation has a finite extent—unlike the Brewer-Dobson
478 circulation in the stratosphere the Hadley cell sinks before reaching the pole—even in the absence of
479 extratropical eddies [*Held and Hou*, 1980]. Second, eddies are important for setting the circulation
480 strength and extent [*Held*, 2000]. Dry models have set the foundations for our understanding of the
481 Hadley cell, but moist processes are critical for determining the width of the ascending branch of the
482 Hadley cell the circulation’s net energy transport.

483 A next logical step in the hierarchy of models to study the Hadley circulation is to include
484 moist effects. One such model is the idealized moist primitive equation of *Frierson* [2007]. This
485 model has a “gray radiation” scheme that neglects cloud and water vapor feedbacks, so that dynamic
486 moisture feedbacks are decoupled from radiative feedbacks. The model uses an idealized large-scale
487 precipitation scheme (condensation upon saturation) and a simple convection scheme that relaxes the
488 atmosphere towards a stable vertical profile. The Hadley cell is very sensitive to the representation
489 of convection. For example, the convection scheme impacts the energetic stratification. The moist
490 static energy difference between the upper- and lower-level Hadley circulation in turn plays a key
491 role in the strength of the mass overturning [*Frierson*, 2007].

492 The idealized model of *Frierson* [2007] can be linked to higher levels of the hierarchy by
493 including more processes. The monsoons and ITCZ, among others problems, can be studied with
494 greater realism by including the seasonal cycle. A second addition is to include the spatial variability
495 in the radiative forcing, and feedbacks, for a more realistic atmospheric energy transport with climate
496 change [*Feldl et al.*, 2017; *Merlis*, 2015]. A third addition is an idealized ocean heat transport
497 coupled to the surface wind stress of the Hadley cell [*Held*, 2001; *Levine and Schneider*, 2011;
498 *Codron*, 2012] that begins to bridge the gap between full-ocean GCMs and slab-ocean boundary
499 conditions. A further extension is to couple the atmosphere and ocean for more realistic ocean
500 heat uptake and transport that results in more realistic atmospheric energy transport by the Hadley
501 circulation [*Zelinka and Hartmann*, 2010; *Feldl and Bordoni*, 2016]. Finally, radiative feedbacks can
502 be introduced to the model by replacing the gray radiation scheme with a more realistic representation
503 or radiative transfer [e.g. *Merlis et al.*, 2013; *Jucker and Gerber*, 2017; *Vallis et al.*, 2018].

504 In addition to understanding the fundamental properties of the Hadley circulation, models
505 such as *Frierson* [2007] are a valuable step in the model hierarchy to investigate how changes in
506 atmospheric water vapor with global warming impact the Hadley circulation. A key science question
507 is: how will the tropical edge change in response to warming? The idealized moist physics GCM
508 has been used to test and extend theories that were originally developed for dry flows [*Held*, 2000]
509 to those that include moisture [*O’Gorman*, 2011; *Levine and Schneider*, 2015]. Furthermore, models
510 such as *Frierson* [2007] have been important for understanding the forced response of the ITCZ,
511 which is formed as a result of converging air toward the equator within the Hadley cell [*Kang et al.*,
512 2009; *Byrne et al.*, 2018].

513 In addition, simplified moist GCMs have been useful to unravel the controls on monsoonal
 514 circulations with the aim to identify the minimal ingredients needed to develop the cross equatorial
 515 tropical overturning circulations that resemble monsoon flow over South Asia. Interestingly, idealized
 516 GCMs can capture aspects of the monsoon without zonally asymmetric land distributions or elevated
 517 orography [Bordoni and Schneider, 2008]. When idealized orography is included, an important
 518 “ventilation” mechanism is revealed: the poleward progression of the monsoon is prevented by mid-
 519 latitude dry air that is blocked by the elevated topography. This mechanism has been found in reduced
 520 vertical structure models, idealized GCMs, and comprehensive GCMs [Chou *et al.*, 2001; Privé and
 521 Plumb, 2007; Boos and Kuang, 2010]. Furthermore, the role of stationary eddies on the monsoons
 522 has been addressed in simulations with idealized lower boundary conditions [Shaw, 2014; Geen
 523 *et al.*, 2018] to assess seasonal circulation transitions in zonally asymmetric GCM configurations.

524 **6 Coupling Clouds and Convection to the Large-scale Circulation**

525 A key simplification of the idealized moist models discussed in Section 5.2 is to leave out
 526 the impact of clouds microphysics on the circulation. Clouds, visible manifestations of atmospheric
 527 convection, play a vital role in the radiative budget, both locally within a single convective system, and
 528 globally: clouds are a key uncertainty in predicting the global temperature response to greenhouse
 529 gas forcing (see Section 6.3). Individual convective clouds can be isolated and appear as random
 530 noise in an otherwise homogeneous environment, such as patchy, fair weather cumulus, but can also
 531 interact with nearby convection and the environment to form mesoscale convective systems such
 532 as squall lines. Organized convection impacts the radiation budget by changing the distribution of
 533 cloudy and clear sky. This is important as the radiative properties of clouds shape the large-scale
 534 circulation of the atmosphere [Hunt *et al.*, 1980; Slingo and Slingo, 1988; Randall *et al.*, 1989].

535 Clouds and convection are also embedded within the large-scale circulation of the atmosphere.
 536 The ascending branches of the circulation cells create the lifting force required for deep convection to
 537 develop within the ITCZ and the descending branches create suppressed regions in which clear sky
 538 or low-level clouds dominate. This two way interaction is referred to as cloud-circulation coupling.
 539 Understanding cloud-circulation coupling, and representing it in models, is one of the World Climate
 540 Research Program’s “Grand Challenges” on clouds, circulation and climate sensitivity [Bony *et al.*,
 541 2015].

542 In Section 6.1 we focus our discussion on Radiative Convective Equilibrium (RCE), a conceptual
 543 model of the tropical atmosphere that has helped us better understand the organization of convection.
 544 In Section 6.2 we discuss a “cloud locking” approach that decouples cloud radiative effects from the
 545 circulation, forming a bridge from the idealized moist GCMs to full atmospheric models. In Section
 546 6.3 we describe how the more complex models within the hierarchy are used to study Earth’s climate
 547 sensitivity.

548 **6.1 Convective Organization: Radiative-Convective Equilibrium**

549 In Section 5.2 we painted a picture of broad ascent within the equatorial branch of the Hadley
 550 circulation, associated with latent heating. This view of tropical precipitation is a reasonable
 551 approximation on longer time scales (weeks or more). On shorter time scale (hours-days), however,
 552 the tropical atmosphere is highly variable, with both ascent and descent in most regions. Convection
 553 on these shorter time scales is organized on small spatial scales, as within a single convective system,
 554 and on large scales, as with the Inter-tropical Convergence Zone (ITCZ) and MJO.

555 Convective organization is not well represented in most atmospheric models [Del Genio, 2012].
 556 This deficiency has been partly attributed to convective parametrizations that have a number of
 557 shortcomings. For example, convection is parametrized in the vertical column without any hori-
 558 zontal interactions, models have limited memory of convection from one time step to the next, and
 559 parametrizations generally do not represent interactions with the (unresolved) mesoscale circulation
 560 [Mapes and Neale, 2011]. A number of persistent model biases have been linked to errors in repre-
 561 senting convection [Randall *et al.*, 2016]. For example, models (i) exhibit too much light rain, which

562 results in insufficient extreme rainfall, (ii) trigger convection too early, resulting in the wrong diurnal
563 cycle, and (iii) often generate a double ITCZ in the central and eastern Pacific [Stephens *et al.*, 2010;
564 Dai, 2006; Sun *et al.*, 2006; Oueslati and Bellon, 2015].

565 The need to improve comprehensive atmospheric models motivates the use of a hierarchy of
566 models to understand, and (ultimately) address long-standing model biases. Models can also be used
567 to improve our theoretical understanding of convection and identify how convection interacts with
568 both the local environment and larger scales [e.g., Muller and Bony, 2015].

569 Radiative-convective equilibrium (RCE) describes a state in which atmospheric radiative cooling
570 is balanced by convective heating in a domain with no externally imposed horizontal structure, e.g.,
571 uniform SST and insolation. RCE was first considered in the 1960s by Manabe and Strickler [1964],
572 who originally proposed it to explain the vertical structure of the atmosphere. Since then, it has
573 evolved into a test-bed for understanding convection in the absence of large-scale circulation. RCE
574 is an important component of a hierarchical approach connecting physical laws to the complex
575 behaviour of the Earth system [Popke *et al.*, 2013]. High-resolution models in RCE are a useful
576 starting point for theories of convective organization [Muller and Bony, 2015].

577 Using a non-rotating cloud resolving model (CRM) in RCE, Bretherton *et al.* [2005] showed
578 that convection can spontaneously self-organize (see Figure 3), a process sometimes known as "self-
579 aggregation". The integration is initialized from a uniform state, and in the first weeks of integration,
580 seemingly random convection is observed homogeneously across the domain. After approximately
581 50 days, however, the system transitions to a single convecting cluster. Self-aggregation is not solely
582 a spatial reorganization of convection; it dramatically changes the mean climate in CRMs resulting
583 in a dryer troposphere, more outgoing long wave radiation (OLR), warmer free troposphere and
584 surface. Please see Wing *et al.* [2017a] for more details and a full list of references, Mapes [2016]
585 for a broader perspective and Holloway [2017] for a comparison to observations.

586 Convection also organizes in RCE simulations using GCMs with parametrized convection, in
587 which large convective clusters form spontaneously [Popke *et al.*, 2013; Reed and Chavas, 2015;
588 Coppin and Bony, 2015; Becker *et al.*, 2017]. Once convection begins to organize, a large-scale
589 circulation develops and helps maintain the convection. In GCMs with prescribed SST, in RCE and
590 non-RCE simulations, convection is more clustered in simulations without parametrized convection,
591 compared to those with active convection parametrizations, and have larger rain rates [Becker *et al.*,
592 2017; Maher *et al.*, 2018].

593 When planetary rotation is included in RCE simulations, self-aggregation transforms into
594 tropical cyclones. Aquaplanet simulations in RCE have been particularly useful for understanding
595 tropical cyclone characteristics [Shi and Bretherton, 2014; Satoh *et al.*, 2016; Reed and Chavas,
596 2015] and their response to increasing SSTs [Held and Zhao, 2008; Khairoutdinov and Emanuel,
597 2013; Merlis *et al.*, 2016]. Satoh *et al.* [2016] used a hierarchy of configurations with a global model
598 to show the multiscale nature of tropical convective systems and how the effects of rotation change
599 the vertical structure of the systems, see Figure 3.

600 The multiscale structure is also apparent in CRM simulations of RCE. The emergent structures
601 remain similar across domain sizes, but the response to perturbations (like imposed surface warming)
602 can vary depending on the domain size [Silvers *et al.*, 2016]. Similar experiments with global models
603 are computationally expensive, but one alternative is to test the convergence characteristics of a
604 model's physics by reducing the planetary radius to mimic increased horizontal resolution; Reed and
605 Medeiros [2016] use this strategy to show how the large-scale convective aggregation seen in GCMs
606 transitions to CRM-like self-aggregation without the increased computational cost.

607 Convective organization more generally is not well understood [Muller and Bony, 2015]. For
608 example it is not clear how important self-aggregation is compared to organization by the mean
609 wind or by waves or other mesoscale disturbances. There are a number of factors that contribute to
610 organization such as cloud-radiative feedbacks, SST and convective-moisture feedbacks, see Sessions
611 *et al.* [2016] for a full list. The model hierarchies has provided insight into why convection organizes

612 and how it is maintained. In this section we have focused on RCE and while it is an idealized model,
613 it is still very complicated.

614 A further useful idealization, complementary to RCE, is the Weak Temperature Gradient
615 (WTG) approximation. Under WTG the large-scale circulation, specifically the vertical veloc-
616 ity, is parametrized [Sobel and Bretherton, 2000; Sobel *et al.*, 2001; Raymond and Zeng, 2005]. This
617 is done by assuming that horizontal temperature gradients and the local time tendency of temperature
618 are both negligible at synoptic scales in the tropics – an observational fact explained dynamically
619 by Charney [1963] – thus reducing the otherwise prognostic temperature equation to a diagnostic
620 equation that can be solved for the large-scale vertical velocity given the diabatic heating. WTG is a
621 horizontal truncation, as opposed to the vertical truncation in the Matsuno-Gill model described in
622 Section 5.1.

623 WTG has been used to study a range of phenomena, including the Walker and Hadley circulations
624 [Bretherton and Sobel, 2002; Polvani and Sobel, 2002; Burns *et al.*, 2006; Bellon and Sobel, 2010;
625 Kuang, 2012]; ENSO teleconnections [Chiang and Sobel, 2002]; tropical cyclogenesis [Raymond,
626 2007] and the MJO [Wang *et al.*, 2013, 2016]. Other related parametrizations of large-scale dynamics,
627 solving the same problem in different ways, have also been developed [Kuang, 2008; Romps, 2012;
628 Herman and Raymond, 2014], and WTG and one other, the ‘damped wave’ method [Blossey *et al.*,
629 2009] applied to a wide range of models in a recent intercomparison [Daleu *et al.*, 2015, 2016].
630 These parametrizations of large-scale dynamics represent the circulation on scales smaller than the
631 global scale at which RCE is relevant – the domain-average vertical motion being parametrized must
632 vanish in RCE by definition – and the domain of a WTG single-column or cloud-resolving simulation
633 can be thought of as representing a small fraction of an RCE simulation’s domain.

634 In such WTG simulations, more than one statistical equilibrium state can occur, depending on
635 the initial humidity, with either dry or persistent deep convection states developing from identical
636 forcing conditions [Sobel *et al.*, 2007; Sessions *et al.*, 2010] depending on initial conditions. These
637 so-called ‘multiple equilibria’ are analogous to self-aggregation in RCE simulations in which a
638 convecting cluster is surrounded by dry subsiding air [Sessions *et al.*, 2016], with the different WTG
639 equilibria representing the convecting and dry regions separately. RCE and WTG together thus form
640 a hierarchy of their own, providing distinct but qualitatively consistent views of the self-aggregation
641 phenomenon.

642 Representing convective organization in Earth system models remains problematic. Progress is
643 being made through a variety of modelling approaches to develop theories of convective organization
644 and to better represent organization in GCM. These approaches cover broad resolutions with high
645 resolutions LES and CRM, and GCMs with different treatments of convection. The convection
646 approaches include: resolved convection in global CRMs [Tomita *et al.*, 2005; Miyamoto *et al.*,
647 2013; Bretherton and Khairoutdinov, 2015; Judt, 2018], with and with parametrized convection
648 [Popke *et al.*, 2013; Maher *et al.*, 2018], and super-parametrization [Arnold and Randall, 2015].

649 **6.2 Decoupling clouds and circulation: Cloud locking**

650 A primary challenge in representing clouds and convection in climate models is to adequately
651 describe the interactions between clouds, convection, and precipitation, which must be parameterized
652 in global models, with radiation and the resolved circulation. One opportunity to explore the role
653 of clouds in the climate system is to adapt the diabatic hierarchy to decouple cloud-radiative effects
654 from the circulation in which they are embedded. A few different approaches have been developed to
655 achieve this: (i) a dry GCM forced with atmospheric cloud-radiative effects simulated from GCMs
656 [Voigt and Shaw, 2016], (ii) reduced-complexity physics (e.g., Frierson-like without clouds [Kang
657 *et al.*, 2009]), (iii) clouds that are transparent to radiation [Stevens *et al.*, 2012], and (iv) prescribing
658 the cloud fields (cloud locking) [Zhang *et al.*, 2010].

659 The cloud-locking model approach has proven particularly helpful to understand how changes in
660 the radiative properties of clouds impact the circulation response to global warming or hemispheric
661 energy perturbations. Cloud-locking removes the coupling between clouds and circulation by pre-

662 scribing the cloud properties seen by the model’s radiation scheme, generally from an earlier model
663 simulation, and this isolates the circulation response to a perturbation as the clouds are invariant
664 [Zhang *et al.*, 2010]. All four modelling approaches listed in the previous paragraph have been used
665 to understand how changes in clouds with increased greenhouse gases will impact the position of
666 the eddy-driven jet [Voigt and Shaw, 2015, 2016; Ceppi and Hartmann, 2016; Ceppi and Shepherd,
667 2017].

668 The eddy-driven jet (discussed in Section 3.4) is an interesting example, as its equatorward
669 bias in coupled GCMs [Kidston and Gerber, 2010] is associated with Southern Ocean clouds that
670 reflect too little shortwave radiation [Ceppi *et al.*, 2012]. Coupled GCMs show diverse responses in
671 the eddy driven jet to global warming, especially in the Southern Hemisphere see Figure 4 a. These
672 broad differences persist in aquaplanet simulations (Figure 4 b), making aquaplanets a desirable
673 configuration to understand the eddy-driven jet response.

674 Cloud-radiative changes lead to a poleward shift in the eddy driven jet in cloud-locking sim-
675 ulations for the MPI-ESM aquaplanet model (Figure 4 c). The cloud-radiative changes with global
676 warming can be attributed to high-level tropical (orange line) and mid-latitude clouds (blue line). In-
677 terestingly, the cloud impact is as large as the differences in jet shifts found in coupled GCMs, which
678 suggests that clouds contribute to uncertainty in future jet shifts. The cloud impact is also repro-
679 duced in the dry Held-Suarez simulations perturbed with radiative changes from the cloud-locking
680 simulations (Figure 4 d).

681 A complementary modelling technique to cloud-locking is the transparent-cloud approach, that
682 prevents the radiation scheme from ‘seeing’ the clouds and hence sets the radiative heating to cloud
683 free conditions [Randall *et al.*, 1989; Merlis, 2015]. This is easier to implement than cloud-locking
684 and is simply achieved by setting the cloud fraction to zero in the radiation scheme. The transparent-
685 cloud approach has helped to demonstrate the importance of cloud radiative effects for the present-day
686 circulation. Such simulations have highlighted that cloud radiative effects strengthen the Hadley cell
687 and eddy driven jet stream, reduce tropical-mean precipitation, and narrow the ITCZ [Li *et al.*, 2015;
688 Harrop and Hartmann, 2016; Popp and Silvers, 2017; Albern *et al.*, 2018].

689 The primary task for understanding the role clouds play in the climate system is to understand
690 their coupling with the circulation, and the implications of that coupling for the circulation response to
691 climate change. In this regard, the transparent-cloud approach has proven helpful for understanding
692 the role of clouds in the present-day climate, and the cloud-locking approach for understanding
693 changes in clouds and circulation with global warming. While recent work has clearly shown that
694 a quantitative understanding of the circulation must consider the coupling to clouds, this remains
695 a rather young area of research with many open research questions, including for example cloud
696 impacts on internal variability of the extratropical circulation [Li *et al.*, 2014].

697 **6.3 The role of circulation in Earth’s equilibrium climate sensitivity**

698 How sensitive is the climate system to greenhouse gas emissions? Clouds are at the heart of
699 this question because they remain the largest source of uncertainty in projections of future climate
700 change. Despite the broad improvements in climate models, early estimates of the equilibrium
701 climate sensitivity – a measure of globally averaged surface temperature change to doubling CO₂ –
702 have not changed since the Charney report in 1979 with a range of 1.5–4.5 K [Stevens *et al.*, 2016].

703 The representation of clouds in different climate models is diverse. This results in widely
704 varying cloud responses to the same perturbation [Boucher *et al.*, 2013; Chung and Soden, 2018].
705 Climate models show a relatively robust positive longwave (infrared/greenhouse) cloud feedback
706 [Zelinka and Hartmann, 2010], attributed to the fixed anvil temperature hypothesis [Hartmann *et al.*,
707 2001; Hartmann and Larson, 2002]. The shortwave (visible/albedo) cloud feedbacks, however,
708 remains highly uncertain despite the fact that most coupled GCMs suggest a weak positive feedback
709 [Ceppi *et al.*, 2017]. Answering the open research questions about climate sensitivity comes down
710 to understanding shortwave feedbacks for low-level clouds which account for much of the model
711 uncertainty in cloud feedbacks. These low-level clouds form below regions of radiative cooling in

712 the descending branches of the Hadley and Walker circulations [Bony and Emanuel, 2005]. As such,
 713 circulation is key in setting their distribution, but cloud effects also feed back on the circulation,
 714 adding complexity to the problem.

715 Single column models (SCMs) have been used to investigate how parametrized physics can
 716 respond to climate sensitivity [Dal Gesso et al., 2015]. Using SCMs with several configurations,
 717 Zhang et al. [2013] showed in idealized climate change experiments that the shallow convection and
 718 boundary layer turbulence are key differences among models. Care must be taken to meaningfully
 719 comparing an SCM to a GCM, however, because of the disconnection of cloud-circulation coupling
 720 in SCMs. In addition, physics packages can exhibit different cloud responses in a GCM and SCMs,
 721 creating obstacles for understanding cloud feedback. Progress has been made to understand cloud
 722 feedbacks in the gap between SCMs and GCMs, such as using WTG to parametrize a circulation in
 723 SCMs [Raymond, 2007; Zhu and Sobel, 2012] and GCMs in RCE to simplify the circulation [Bony
 724 et al., 2016; Popke et al., 2013; Wing et al., 2017b] – in a conceptually similar way to Manabe and
 725 Strickler [1964] who used SCMs.

726 To capture the impact of circulation on climate sensitivity, efforts have focused at the top
 727 of the model hierarchy: coupled atmosphere-ocean GCMs (AOGCM) [Otto et al., 2013; Stevens
 728 et al., 2016; Caldwell et al., 2016]. This is because simpler models make severe assumptions about
 729 the system, removing non-linear behavior that may project on to climate sensitivity [Knutti and
 730 Rugenstein, 2015]. From the perspective of the model hierarchy, AOGCMs are a moving target
 731 that evolves in response to both improvements in our understanding of the climate system, and to
 732 increasing computational resources.

733 The complexity of modern climate models, however, make it challenging to interpret their
 734 results, including the relative role of cloud feedbacks in climate change. The challenges in under-
 735 standing climate sensitivity in AOGCM makes a hierarchical approach appealing. The goal then
 736 becomes understanding the response of state-of-the-art AOGCMs in a simpler setting to reveal the
 737 underlying mechanisms and improve our physical understanding of the system. For example, using
 738 a range of boundary conditions and model configurations (ESM, GCM, aquaplanet, SCM) with the
 739 same model parametrizations, Briant and Bony [2013] identified a positive feedback that depends on
 740 how moist static energy is transported between the free troposphere and the boundary layer. Progress
 741 has been made using aquaplanet simulations to identify shallow cumulus clouds as driving the spread
 742 in climate sensitivity [Medeiros et al., 2008; Ringer et al., 2014; Medeiros et al., 2015].

743 **7 Case study: The Madden–Julian Oscillation**

744 In Sections 5-6 we described the models that have been fundamental for advancing our under-
 745 standing of tropical circulation and the important role that moisture plays in setting the circulation,
 746 specifically how convective organization and clouds impact the radiative structure of the atmosphere.
 747 In this section we will focus our attention the Madden-Julian Oscillation (MJO). The MJO is an
 748 organized convective system and the primary source of tropical intraseasonal variability. The MJO
 749 continues to challenge our understanding of how circulation couples to clouds, convection and ra-
 750 diation. Progress in being made in our theoretical understanding of the mechanisms that initiation,
 751 propagate and maintain the MJO, however, there is currently no complete theory for the MJO [Ahn
 752 et al., 2017]. As a result, the MJO is generally poorly represented in comprehensive climate models.
 753 In this review, we use the MJO as a case study to highlight how the model hierarchies—in particular
 754 idealized models—have been used to progress our understanding, develop new theories and improve
 755 the representation of the MJO in comprehensive models.

756 The MJO is an envelope of organized tropical convection that drifts eastward from the Indian
 757 Ocean into the Pacific. It is distinct from most convectively coupled equatorial waves in having
 758 a relatively slow speed of propagation ($\approx 4\text{--}8$ m/s), longer timescales (about 1–2 months), and a
 759 relatively large scale (planetary wavenumbers 1–3) in comparison to other synoptic disturbances in
 760 the tropics. While it has also been historically difficult to simulate in global models, some recent

761 models do much better. For the first time, some dynamical forecasts are now superior to statistical
762 ones. This new simulation capability allows theoretical ideas to be tested.

763 Realistic simulations of the MJO require convection to be sensitive to free-tropospheric moisture,
764 i.e., a positive moisture-convection feedback, where deep convection is favored in regions where free-
765 tropospheric humidity is higher. CMIP5-class models with the largest moisture sensitivity tend to
766 have the most realistic MJO [Kim *et al.*, 2014a]. Poor simulations of the MJO — generally those
767 with weak to non-existent MJOs [Ahn *et al.*, 2017] — can be improved by increasing the sensitivity
768 of convection to moisture, such as increasing the entrainment and rain re-evaporation. Such tuning to
769 optimize the MJO generally causes biases in mean climate [e.g., Kim *et al.*, 2011], but there is some
770 evidence to suggest a realistic MJO and mean state can occur simultaneously even with traditional
771 convection schemes [Crueger *et al.*, 2013]. There is considerable additional evidence, apart from the
772 MJO, that deep convection in general is quite sensitive to moisture [e.g., Derbyshire *et al.*, 2004], and
773 that typical convective schemes have excessive undilute ascent, as opposed to entraining air about
774 them [e.g., Tokioka *et al.*, 1988; Kuang and Bretherton, 2006].

775 More recent studies have viewed the MJO through the moist static energy budget where surface
776 fluxes and radiation are the dominant source terms (since moist static energy is conserved under
777 condensation, which is the dominant source term in the dry static energy budget in deep convective
778 conditions). Feedbacks between surface turbulent fluxes and convection were emphasized in early
779 theories [Neelin *et al.*, 1987; Emanuel, 1987] and appear to be important in some GCMs [e.g.
780 Maloney and Sobel, 2004]. Other work, however, points to a key role for cloud-radiative feedbacks;
781 for example, there is less longwave cooling by high-clouds in a moist atmosphere [Andersen and
782 Kuang, 2012; Chikira, 2013]. Process-based diagnostics [Kim *et al.*, 2015] and so-called “mechanism
783 denial” experiments [Kim *et al.*, 2012; Crueger and Stevens, 2015; Ma and Kuang, 2016] in which
784 a process is removed in order to test its importance, have lead to progress. This is consistent with
785 earlier work with more idealized models. Raymond [2001] argued that radiative feedbacks were
786 important to the MJO based on results from a 3D model of intermediate complexity, while Bony and
787 Emanuel [2005] did so based on 2D CRM simulations without rotation. In an even simpler context,
788 Hu and Randall [1994] found radiative feedbacks are critical in a one-dimensional model without
789 large-scale circulation.

790 The importance of moisture-convection and cloud-radiative feedbacks suggests a view of the
791 MJO as essentially a form of self-aggregation on the equatorial θ -plane, in a domain much larger
792 than CRMs simulations [e.g. Arnold and Randall, 2015]. In aquaplanet simulations with super-
793 parametrized convection in RCE, Arnold and Randall [2015] found similar energy budgets and
794 radiative feedbacks in non-rotating simulations, where self-aggregation dominates, and simulations
795 with rotation, where MJO-like variability occurs.

796 The importance of moisture-convection and cloud-radiative feedbacks are the core assumptions
797 in a recent set of highly idealized models of the MJO. These models represent the MJO as a
798 moisture mode – a mode that would be absent in a dry atmosphere. In these idealized models,
799 essential information is contained in the moisture field. Truncation to a single vertical mode, as in
800 the Matsuno–Gill model, allows the dry dynamics to become shallow water-like. The convection
801 schemes depend strongly, and in some cases exclusively on the moisture field, building in a strong
802 moisture-convection feedback.

803 Moisture modes emerged in the idealized models of Fuchs and Raymond [Fuchs and Raymond,
804 2002, 2007; Raymond and Fuchs, 2007, 2009]. The moisture mode was isolated in the simple 1-D
805 linear model of Sobel and Maloney [2012, 2013] that has a single moisture prognostic variable,
806 assumes WTG in the temperature equation, and generates winds by assuming a Matsuno–Gill
807 response to quasi-steady heating (approximately valid as long as the disturbance does not propagate
808 too quickly). In this model it can be shown explicitly that radiative feedbacks are critical for eastward
809 propagation in a linearly unstable mode [Sobel and Maloney, 2013]. While the eastward propagation
810 was initially slower than observations, modifications by Adames and Kim [2016] increased the
811 propagation speed by accounting for meridional moisture advection. Because the WTG assumption
812 eliminates the Kelvin waves, the waves that most early theories relied on to explain the eastward

813 propagation, the propagation of a moisture mode results largely from horizontal moisture advection,
 814 which seems to be supported by a number of observational and modeling studies [e.g., *Maloney,*
 815 *2009; Pritchard and Bretherton, 2014; Kim et al., 2014b; Inoue and Back, 2015a*].

816 Moisture mode theory — including the link to self-aggregation in idealized simulations —
 817 provides a useful framework for diagnosing models and observations, although whether moisture
 818 mode models correctly capture the MJO remains a topic of debate. The moisture mode ideas are
 819 quite different from those in earlier MJO theories, most of which excluded both radiative feedbacks
 820 and prognostic moisture (e.g., see review by *Wang [2005]*), and also differ from other, more recent
 821 models [e.g., *Majda and Stechmann, 2009; Yang and Ingersoll, 2013*]. Now that some comprehensive
 822 models at the top of the model hierarchy can simulate the MJO with reasonable fidelity, it is a question
 823 of linking them to our theories of MJO behavior. A connection to the moisture mode hypothesis, for
 824 example, can be traced through a hierarchical chain from self-aggregation in idealized simulations
 825 to more realistic simulations where moisture-convection and radiative feedbacks are allowed.

826 **8 Synthesis and Outlook**

827 *All models are wrong but some are useful.* The statistician George Box succinctly made two
 828 points at a workshop on statistical robustness four decades ago [*Box, 1978*]. First is the reminder
 829 that all of our models, even the most sophisticated, are inherently simplified – and so in Box’s sense
 830 “wrong” – and thus unable to capture all the potentially relevant processes and scales of the climate
 831 system. But second, we can learn, understand, and make predictions with *some* models.

832 In this review, we have identified a number of deliberately simplified models that have proven
 833 useful for understanding and predicting the large scale circulation of the atmosphere. We have
 834 not identified all possible benchmark models, but have sought to provide a balanced view of the
 835 dynamics of the tropical, extra-tropical, and middle atmosphere, highlighting processes on scales
 836 large, e.g., planetary waves in the Holton–Mass model, to small, e.g., convection and clouds within
 837 radiative-convective equilibrium integrations.

838 In Section 2, we proposed three principles to help organize models into hierarchies: dynamics,
 839 process, and scale. These are motivated, in part, by decisions we make in order to create a numerical
 840 model of the atmosphere that captures the large-scale circulation. These decisions include the
 841 appropriate governing equations, the relevant processes that drive the circulation, and the domain
 842 and resolution (which determine the allowable scales). These principles are not independent of one
 843 another. Dynamical hierarchies are designed to isolate particular scales and processes, e.g., the
 844 quasi-geostrophic equations focus on Rossby wave processes by filtering out the faster and smaller
 845 scale gravity waves. Likewise, the process hierarchy influence the choice of dynamics; if we wish
 846 to look at non-hydrostatic effects, we must resolve scales with an order-one aspect ratio, and thus
 847 the kilometer scale. The models featured in Sections 3-7 provide several examples of each of these
 848 hierarchies that have organically emerged in the literature, as highlighted in Figure 5.

849 Dynamical hierarchies have played a key role in understanding the mid-latitude circulation,
 850 where fast rotation and stratification organize the flow. We define the **equation hierarchy**, see
 851 Figure 5, that forms a natural progression of the equation set. The equation hierarchy includes
 852 the (i) barotropic vorticity dynamics that capture the evolution of Rossby waves (Section 3.1), (ii)
 853 quasi-geostrophic flow on 2 or more layers that generally captures baroclinic instability (Section
 854 3.2), (iii) the dry primitive equation dynamics, e.g., as represented in the the Held-Suarez model,
 855 (iv) the moist primitive equation dynamics (as in the Frierson model in Section 5.2 or a standard
 856 AGCM), and ending with (v) the non-hydrostatic equations that includes the vertical momentum
 857 equation and are accurate at higher horizontal resolutions, e.g. used in CRMs or weather forecast
 858 models. In the tropics, rotation is weak and moist processes are of first order importance. As such,
 859 the dynamical hierarchies generally only include the more complex end of the equation hierarchy.
 860 None-the-less, the primitive equations or non-hydrostatic dynamics can be used with either vertical
 861 truncation (Matsuno-Gill model in Section 5.1) or horizontal truncation (weak-temperature gradient
 862 approximation in Section 6.1) to simplify the equation set.

863 The focus on processes is most essential for organizing model hierarchies. The purpose of the
 864 dynamics and scale hierarchies are then used to isolate and resolve the processes of interest. An
 865 example of a process hierarchy is the **diabatic hierarchy**, a term we use to describe a series of
 866 GCMs that integrate the primitive equation dynamics on the sphere, with advancing representations
 867 of the processes driving the temperature equation and generally with a resolution on the order of 100
 868 km. At the base of the diabatic hierarchy is (i) the *Held and Suarez* [1994] model (often referred
 869 to as a dry dynamical core) where all diabatic processes are replaced by Newtonian temperature
 870 relaxation. The Held-Suarez model has been used to understand jet stream variability (Section 3.4),
 871 tropical overturning circulation (Section 5.2), stratosphere-troposphere coupling (Section 4.1), and
 872 tracer transport (Section 4.3).

873 The next step in the diabatic hierarchy is to add moisture using a (ii) "gray" radiation schemes.
 874 This scheme decouples the convective latent heating from the radiation scheme so that water vapour
 875 is transparent to the radiation scheme [e.g., *Frierson et al.*, 2006; *O’Gorman and Schneider*, 2008].
 876 The next step in the diabatic hierarchy is (iii) to include a full radiation in the absence of clouds (or
 877 with a prescribed cloud climatology) that allows water vapor to interact with radiation in a simplified
 878 context [e.g., *Merlis et al.*, 2013; *Jucker and Gerber*, 2017]. These models have elucidated the
 879 circulation of the tropics and coupling between high and low latitudes (Section 5.2). At the next
 880 step in the diabatic hierarchy are (iv) atmospheric General Circulation Models that account for the
 881 importance of cloud and aerosol processes in the diabatic forcing of the circulation (Section 6).
 882 The most complex end of the diabatic hierarchy is to include the (v) carbon cycle and interactive
 883 chemistry which enables a more realistic representation of the processes governing radiative gases,
 884 clouds, and aerosols. The complex end of the diabatic hierarchy continues to evolve with time, as
 885 more processes are included in Earth System models and computational resources continue to grow.

886 Another process hierarchy that helps to organized the model hierarchies focusses the lower
 887 boundary conditions. Atmospheric models can be created with oceans that have (i) constant or fixed
 888 SST, (ii) aquaplanets with a so-called “slab” ocean which only captures the local thermodynamics
 889 of the atmosphere-ocean coupling, and (iii) a slab ocean with q-fluxes which include idealized
 890 horizontal transport. These models can also be configured to have idealized land and topography
 891 by changing the heat capacity and boundary layer roughness. The representation of the land surface
 892 conditions can be idealized or more realistic e.g., bucket hydrology vs. water runoff or a full
 893 representation of vegetation, aerosols, and carbon chemistry. The atmospheric models can also be
 894 forced with (iv) observed SSTs or (v) with an interactive ocean (vertical and horizontal) to form a
 895 coupled atmosphere-ocean model.

896 Figure 6 illustrates a hierarchy available within the CESM framework, incorporating elements
 897 of both the diabatic hierarchy and varying configurations of the land surface. The SimpleER project
 898 [*Polvani et al.*, 2017] makes many of these models an integral part of the CESM structure. The
 899 Isca framework [*Vallis et al.*, 2018], based on the GFDL modeling system, includes many of the
 900 lower steps of the hierarchy, but also includes hooks to add complexity and to build models of other
 901 planetary atmospheres as needed. One aspect of the process hierarchy that moves beyond these
 902 GCMs is to include more comprehensive treatments of microphysical processes that determine the
 903 distribution of clouds. An example is the Weather Research and Forecasting (WRF) model, which
 904 offers different options for representation of atmospheric processes, such as microphysics, and the
 905 treatment of boundary conditions.

906 Our final principal for organizing the models is scale. One example in which a hierarchy has
 907 naturally developed is for studying convective organization (Section 6.1). The model domain can vary
 908 from very high resolution in a small domain (to understand in-cloud properties) to low resolution
 909 on a global scale to understand planetary scale organization such as the MJO. Scale hierarchies
 910 are also implicit in dynamical hierarchies. Simplified models have proven useful in problems that
 911 intrinsically involve a great spread in scales, such as the QBO, where the evolution of planetary scale
 912 jets is driven by small scale gravity waves, and could only recently be captured in AGCMs.

913 Looking forward, we believe that model hierarchies will continue to help us improve climate
 914 and weather models. In particular, the gap in our understanding of the coupling processes between

915 clouds, convection, and circulation is mirrored in part with a gap in simple models that isolate the key
916 processes regulating these interactions. There is a large jump between idealized moist models that
917 effectively neglect cloud-aerosol processes [e.g., *Frierson et al.*, 2006; *Merlis et al.*, 2013; *Jucker*
918 *and Gerber*, 2017] and comprehensive GCMs that seek to parametrize all the unresolved scales
919 which are critical to clouds and aerosols. This gap partially reflects the difference between what
920 can be done by an individual research group and a full modeling center. Further development of
921 simpler GCMs that capture the essential elements of cloud and aerosol interactions are needed. It
922 requires identifying sufficiently elegant model configurations, in the language of *Held* [2014], that
923 would merit investment by a modeling center, or consortium of research groups, to bring in sufficient
924 expertise.

925 Radiative-convective equilibrium integrations are in part aimed at this gap between large scale
926 dynamics and clouds processes. There is still a fundamental separation between them and the
927 real atmosphere, however, where wind shear plays a vital role in organizing convection. This
928 gap is visually emphasized in Figure 6 by the profound changes in circulation in CESM between
929 simulations in RCE and an aquaplanet model (where the large-scale flow is determined by rotation
930 and the temperature). Adding the building blocks of rotation and shear into RCE integrations may
931 help establish these links.

932 In this review we have highlighted various ‘benchmark’ models for understanding and modelling
933 the large-scale circulation of the atmosphere. We emphasize that their *connectedness* is essential;
934 indeed it is what defines a hierarchy. A simple model must be connected in some way to a compre-
935 hensive model and/or to reality for it to have value, else it becomes irrelevant. Connectedness does
936 not always need to occur in a sequence of small steps; in some cases a simple model may connect
937 almost directly to observations or experiment (the Lindzen–Holton–Plumb model of the QBO may
938 be an example). However, such a leap is the exception, and in most cases a simple model connects
939 to reality via a sequence of other models.

940 Model hierarchies will continue to play a role in our understanding of climate projections; in
941 fact, we argue they should play an increasingly important role. We do not believe in global warming
942 because a GCM tells us it is so; rather, we believe in it because of very basic physical laws. However,
943 in their simplest manifestation those laws have little quantitative predictive capability for Earth’s
944 climate. At the other extreme, when comprehensive models are forced into the warmer regimes
945 that may lie in our planet’s future, we do not have the ability to compare parametrizations with
946 observations. A purposes of the model hierarchies is then to provide a pathway connecting robust
947 physical laws to our complex reality, via models of varying levels of complication. Ideally, this
948 enables us to both understand the processes involved and to make useful and trustworthy predictions.

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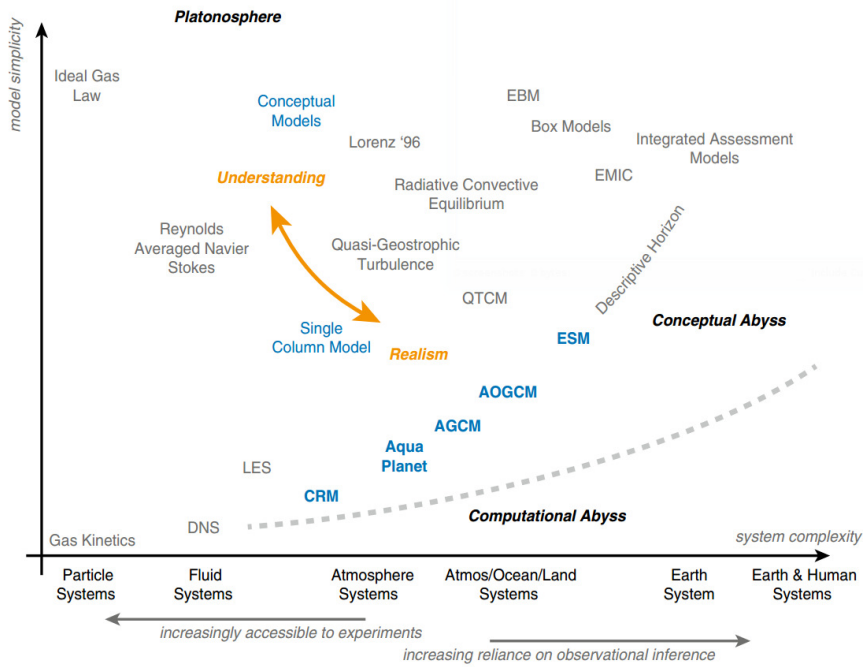
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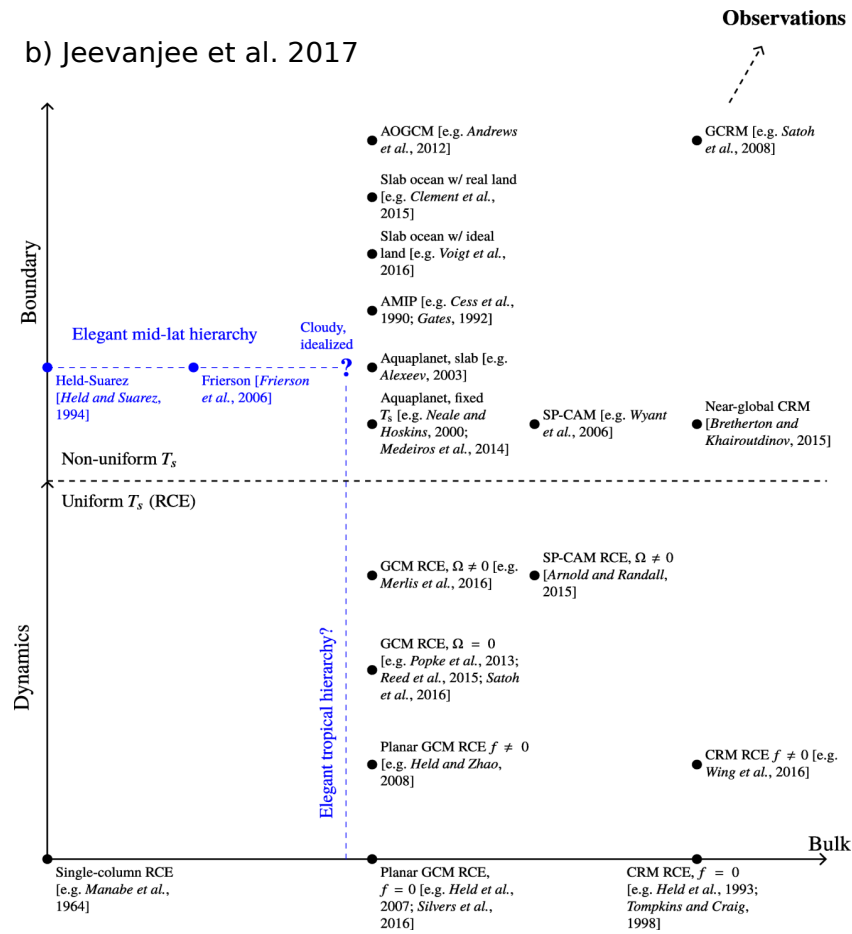
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a) Bony et al. 2013



b) Jeevanjee et al. 2017

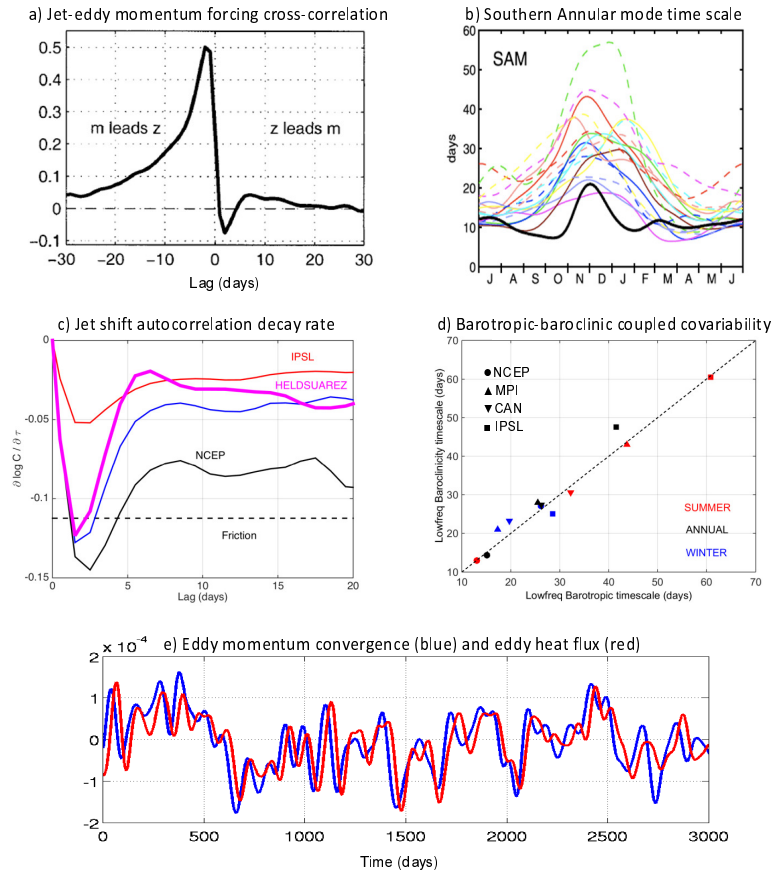


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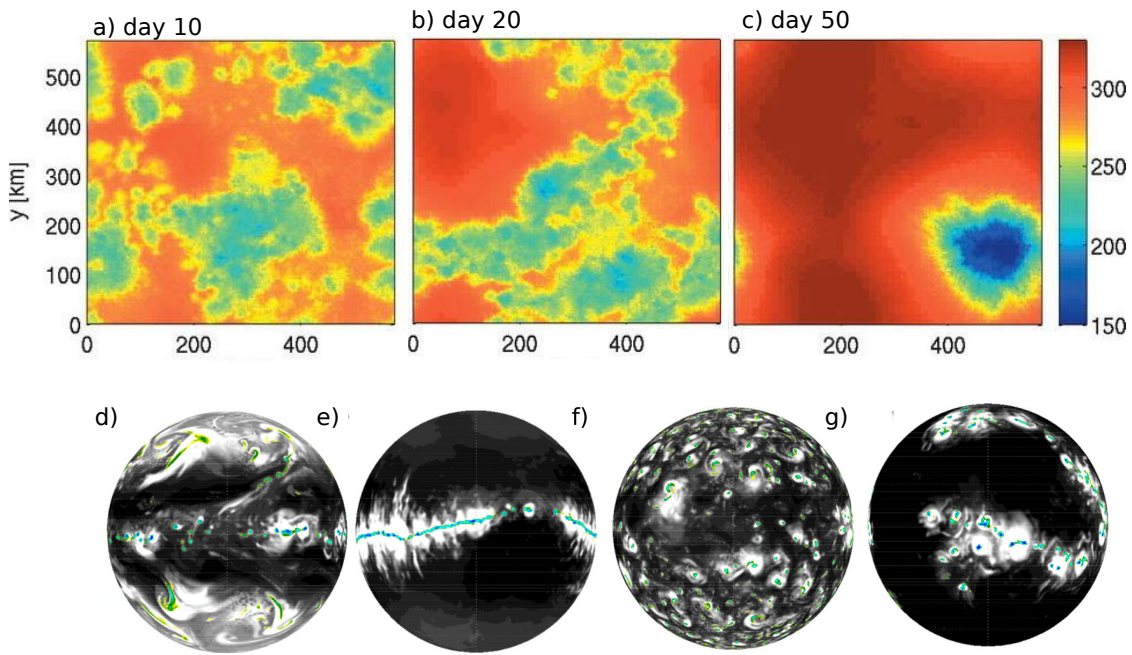
Figure 1. Categorizing atmospheric climate models in terms of complexity a) from *Bony et al.* [2013] and b)

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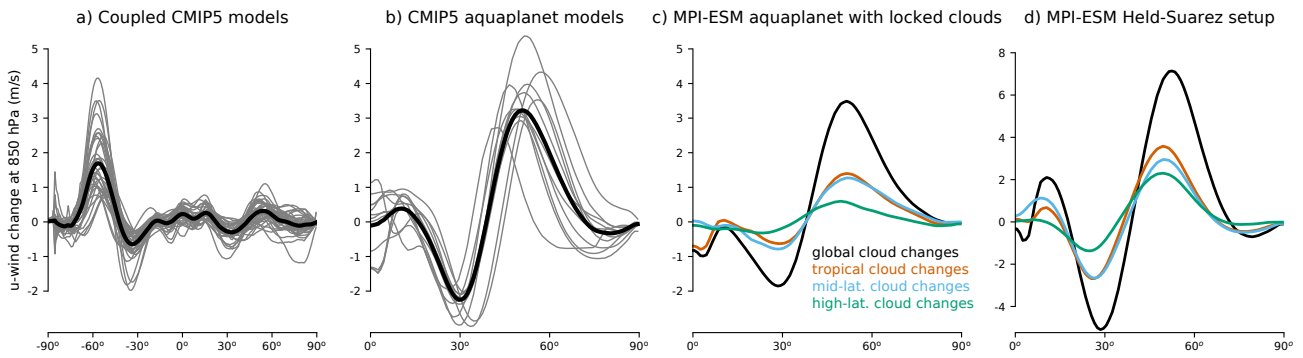
grouped in terms of model configurations for Earth's climate as in *Jeevanjee et al.* [2017].



1575 **Figure 2.** (a) Lagged correlation between zonal mean wind (z) and eddy momentum forcing (m) from
 1576 *Lorenz and Hartmann* [2001]. (b) Autocorrelation timescale of the Southern Annular Mode for observations
 1577 (black thick solid) and CMIP3 models (colors), adapted from *Gerber et al.* [2008]. (c) Logarithmic decay rate
 1578 of autocorrelation for zonal wind anomalies in observations (black), two CMIP5 climate models (IPSL: red,
 1579 CAN:blue) and the Held and Suarez model (magenta). (d) Scatterplot between low-frequency logarithmic decay
 1580 rates of baroclinicity and barotropic wind anomalies (average from 5-20 day lags) for the models and seasons
 1581 indicated. (e) Sample timeseries of the low-frequency eddy momentum (blue) and heat (red) flux contributions
 1582 to the upper-layer Eliassen-Palm divergence in the QG simulations of *Zurita-Gotor et al.* [2014]



1583 **Figure 3.** Radiative-Convective Equilibrium simulations in a CRM: top panel is daily OLR for a fixed SST
 1584 (301K) run after a) 10, b) 20 and c) 50 days of the simulation, adapted from *Bretherton et al.* [2005]. The
 1585 bottom panel is OLR for high resolution GCM aquaplanet stimulations using zonally symmetric SSTs similar to
 1586 observation d) with rotation (Earth like), e) without rotation, and uniform SSTs f) with and g) without rotation
 1587 (RCE case), adapted from *Sato et al.* [2016].



1588 **Figure 4.** Extratropical cloud-circulation coupling. The impact of clouds on the eddy driven jet stream
 1589 response to global warming in a hierarchy of GCMs. The zonal-mean time-mean change in 850 hPa zonal
 1590 wind (ms^{-1}) for each latitude ($^{\circ}$) for the ensemble mean (bold line) and individual models (gray) for a) CMIP5
 1591 coupled Earth system models with $4\times\text{CO}_2$ and b) aquaplanet CMIP5 models with prescribed-SST and 4 K SST
 1592 warming. For the MPI-ESM model in aquaplanet prescribed-SST setup, simulations with the cloud-locking
 1593 method and imposed global (black) and regional (colors) cloud changes show the cloud-radiative contribution
 1594 to the eddy driven jet response to warming (panel c). The global and regional cloud impacts are reproduced in
 1595 panel d) using a dry Held-Suarez setup of the MPI-ESM model perturbed with the radiative forcing from cloud
 1596 changes of panel c. Because panels b-d are for aquaplanet simulations, only the Northern hemisphere is shown.
 1597 Note the different y-scale in panel d, which reflects the increased jet sensitivity of the Held-Suarez setup. Figure
 1598 adapted from *Voigt and Shaw* [2016].

dynamical (equation)

barotropic
quasi-geostrophic
dry primitive equations
moist primitive equations
non-hydrostatic



process (diabatic)

dry dynamical core
moist model gray radiation
full radiation without clouds
prescribed clouds and aerosols
interactive chemistry



process (boundary condition)

constant SST
slab ocean
slab ocean with q-fluxes
observed SST with land (AMIP)
coupled ocean-atmosphere with land

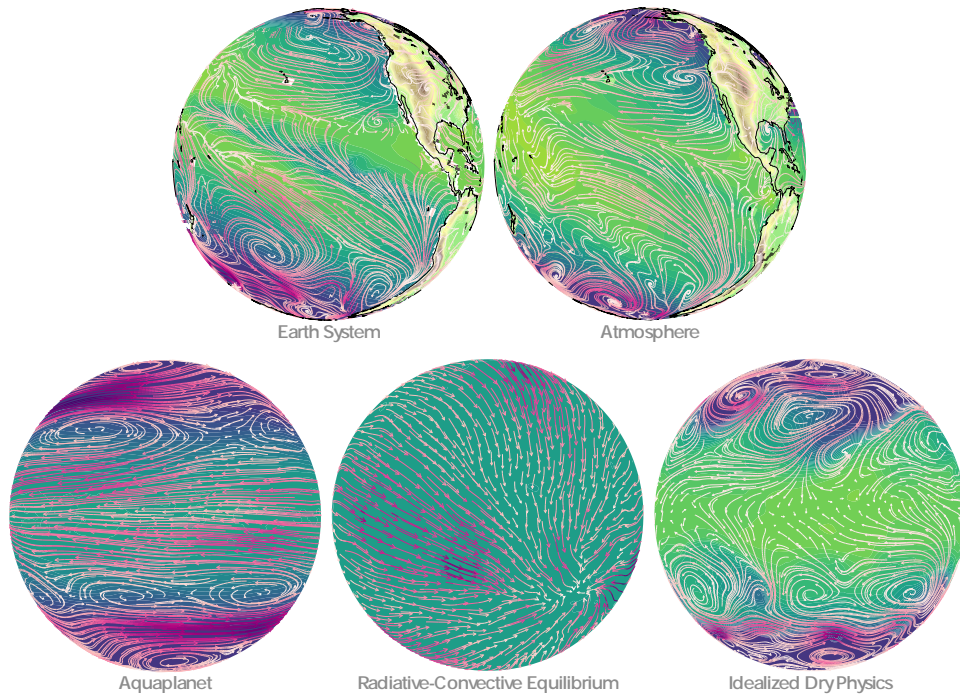
**Hierarchies for
atmospheric circulation**

scale (convective organization)

turbulence
cloud scale
cloud system
mesoscale convective systems
synoptic to planetary scale

Maher et al. 2019

1599 **Figure 5.** The three principles view of the model hierarchies used for understanding the large-scale circulation.
1600 The dynamical hierarchy is shown in terms of the equation hierarchy. The process hierarchy is described in
1601 terms of a diabatic hierarchy and the boundary conditions. Convective organization is used as an example to
1602 illustrate the scale hierarchy. For each list, the first element is the simplest or smallest-scale and builds down to
1603 the most complex or largest-scale. This is an example to illustrate the concept of the three principles and does
1604 not capture all the available models.



1605 **Figure 6.** Models available within the hierarchy in the CESM system. (Top) The Earth system model and
1606 atmosphere only models (with prescribed SST). (bottom) Aquaplanet, RCE and idealized dry physics. The
1607 colour contours over the ocean are SST and over land topography. Streamlines are the near-surface wind
1608 (thicker lines are stronger winds). Each globe is a monthly mean except for the idealized dry model which is a
1609 snapshot.