



## ABSTRACT

11 Blocking is a persistent, large-scale circulation pattern in the mid-latitude atmosphere associated  
12 with extreme weather at the surface. Identifying and understanding the temporal evolution of blocks  
13 is not only important for enhancing our capability to predict them, but also for shedding light on  
14 whether atmospheric blocking is a distinct meteorological phenomenon. This study examines the  
15 recurrence, or return period distribution of blocking in the Northern Pacific, Northern Atlantic,  
16 and Southern Pacific regions for both warm and cold seasons. Using ERA5 reanalysis data and  
17 Community Earth System Model Large Ensemble (CESM LENS) outputs, this study finds that  
18 blocking events are typically separated from each other on a timescale of 8-12 days, which is robust  
19 across regions and seasons. The recurrence distributions are interpreted with a hierarchy of one and  
20 two dimensional stochastic models. The idealized models indicate that the variation in blocking  
21 recurrence depends on the climatological onset frequency of blocking events and the characteristic  
22 temporal correlation of Rossby waves. The return period distributions in reanalysis and CESM are  
23 consistent with an AR(1) autoregressive process of order 1 model, suggesting that the temporal  
24 structure of blocks can be interpreted as red noise associated with synoptic variability. Using the  
25 CESM LENS outputs, the authors find that the decline in blocking frequency in a warmer climate  
26 leads to a broader spread of the return-period distribution, increasing variance in the recurrence of  
27 blocks.

28 *Significance statement.* Atmospheric blocking is a large-scale weather pattern in the midlatitudes  
29 associated with various types of extreme events, such as heat waves, droughts, and cold spells.  
30 Understanding its regularity in time can help us better predict its onset and understand the forecast  
31 limit of blocking. Using a hierarchy of simple red-noise models, we identify the key parameters that  
32 contribute to the recurrence pattern of blocking, specifically, the climatological onset frequency  
33 and the temporal correlation of Rossby waves, which shape the return period distribution and  
34 timescale. These insights also help interpret changes in the pattern of recurrence and forecast  
35 challenges in a warmer climate from the CESM1 simulations, where a decrease in blocking events  
36 increases the uncertainty of their recurrence.

## 37 **1. Introduction**

38 Atmospheric blocking is an important phenomenon characterized by the stagnation of propagat-  
39 ing weather systems and often leads to surface extremes (Kautz et al. 2022) such as heat waves  
40 (Brunner et al. 2018; Neal et al. 2022; Pfahl and Wernli 2012), cold spells (Brunner et al. 2018;  
41 Demirtaş 2017), and extreme precipitation. As blocks occur on a timescale longer than the typical  
42 synoptic weather, but shorter than seasonal variations, understanding their temporal evolution can  
43 help bridge the gap between weather and climate extremes and mend the weather-climate schism  
44 (Randall and Emanuel 2024). Current short- or medium-range forecasts do not adequately predict  
45 blocks, making extremes more dangerous, especially in a changing climate (Intergovernmental  
46 Panel On Climate Change 2023).

47 The spatial distribution of blocks is well-understood: in the Northern hemisphere, blocks are  
48 found more frequently over the Northern Pacific, Northern Atlantic, and Greenland (Dole and  
49 Gordon 1983; Tyrlis and Hoskins 2008; Woollings et al. 2018). In the Southern Hemisphere,  
50 blocks are primarily observed over the South Pacific (Liu and Wang 2024). However, less is known

51 about the temporal features of blocks. As a recent Perspective (Wang et al. 2026) pointed out,  
52 among blocking detection algorithms, nearly all identify blocks when the usual westerly flow is  
53 blocked in a region for five days or more. Beyond the 5-day temporal threshold for blocks, however,  
54 we do not have much understanding of the temporal features of blocks. This study aims to provide  
55 more insight of blocking events by exploring the regularity in its occurrence. We ask how blocking  
56 events are interspersed in time, whether there is more regularity than weather noise, and how this  
57 variability differs among regions, and between observations and models.

58 The presence of any regularity in blocking occurrence would help us to understand the funda-  
59 mental processes behind the phenomenon. For example, if blocks are driven primarily by feedback  
60 processes from random synoptic eddies' (Shutts 1983), then a null-hypothesis is that their temporal  
61 structure is largely random, their onset following the distribution of synoptic eddies, but with  
62 events exhibiting extended persistence due to the self-sustaining nature of the blocks. This begs  
63 the question, how do blocks differ from random noise? By definition, blocks are larger in size and  
64 longer lasting than random eddies, as well documented in classic diagnostic works, e.g. Dole and  
65 Gordon (1983). But if the main distinctions between blocks and individual weather systems are just  
66 size and duration, the distinction would be purely semantic rather than fundamental. Masato et al.  
67 (2009) demonstrated that a simple first-order Markov model, with observed coherence included in  
68 its formulation, can reproduce the main features of blocking frequencies. The only exception is that  
69 observed blocks appear to be more persistent than predicted by the first-order Markov model. Re-  
70 cent studies have shown the importance of diabatic heating (Pfahl et al. 2015; Liu and Wang 2025)  
71 and baroclinic energy exchange from synoptic systems (Martineau et al. 2022) in the maintenance  
72 of block.

73 In exploring the temporal patterns of atmospheric blocking, earlier studies have linked blocking  
74 with various internal modes of variability, which include the zonal wind cycle (Namias 1950;

75 Rossby 1939), Northern Annular Mode (Tachibana et al. 2010; Thompson and Wallace 2000) and  
76 North Atlantic Oscillation (Scherrer et al. 2006). Liu and Wang found that the Baroclinic Annular  
77 Mode (BAM), a leading mode of storm activity with a periodicity of 20-30 days, modulates the  
78 frequency of atmospheric blocking (Liu and Wang 2023; Liu 2023). The alignment of blocking  
79 with a periodic annular mode implies that blocking occurrence may exhibit more regularity than  
80 red noise. Indeed, blocks and associated extremes are associated with slowly propagating Rossby  
81 wave packets with an intrinsic timescale of 10 days (Castañeda and Wang 2024; Röthlisberger  
82 and Martius 2019; Teng et al. 2013; Wirth et al. 2018). Despite evidence suggesting potential  
83 regularity in blocking occurrence, the temporal variability and recurrence of blocks have not yet  
84 been systematically examined. It remains unclear whether blocks exhibit a characteristic return  
85 period and how this compares with that of typical synoptic eddies. Recognizing the preferred  
86 recurrence of blocks at specific timescales could potentially provide a largely underexploited  
87 intrinsic predictability of blocks and improve medium-range weather forecasts in current and future  
88 climates. Further, this could provide key ingredients for us to re-think the first-order dynamics of  
89 atmospheric blocking. This work investigates the recurrence of blocks based on observations and  
90 a climate model, aided by insights from simple red noise models.

91 We evaluate to what extent blocking exhibits a regular recurrence pattern in several key regions  
92 of blocks, including the Northern Pacific, Northern Atlantic, and Southern Pacific regions, in both  
93 warm and cold seasons, and we compare the statistics to those in two simple red noise models: the  
94 2-D model of Masato et al. (2009) and an even simpler 1-D model. The methodology, including  
95 blocking detection, corresponding return period calculation, and red noise model construction, are  
96 elaborated in Section 2, followed by a discussion of the results from observation, climate model,  
97 and red noise models in Section 3. Our conclusions are in Section 4.

## 98 2. Data and Methods

### 99 *a. Reanalysis and Climate Model Outputs*

100 The blocking analysis performed in this study uses the ERA5 reanalysis dataset from the European  
101 Centre for Medium-Range Weather Forecasts (ECMWF, Hersbach et al. 2020). We use the daily  
102 mean geopotential height field at 500 hPa (Z500) from 1 January 1940 to 31 December 2022 with  
103  $1^\circ \times 1^\circ$  horizontal resolution to diagnose blocking events. We also evaluate historical and potential  
104 future changes in blocking recurrence using daily model outputs from the Community Earth System  
105 Model version 1 (CESM1). We analyze blocks from the LENS integrations of the fully-coupled  
106 CESM1 under preindustrial radiative forcing, as well as future climate scenarios (RCP 8.5), with  
107 30 ensemble members each (Deser et al. 2020).

### 108 *b. Blocking Detection and Return Period Calculation*

109 To analyze blocking events, we calculate the Local Wave Activity (LWA) by integrating the  
110 meridional displacement of the Z500 contour (Chen et al. 2015; Huang and Nakamura 2016),

$$LWA_{Z500}(t, \phi, \lambda) = \frac{a}{\cos \phi_{eq}} \left( \int_{\phi \leq \phi_{eq}} z' \cos \phi d\phi - \int_{\phi \geq \phi_{eq}} z' \cos \phi d\phi \right) \quad (1)$$

111 where  $a$  is the radius of the earth,  $\phi_{eq}$  is the equivalent latitude. The equivalent latitude encloses  
112 the same area for a given Z500 contour.  $z'$  denotes the deviation of Z500 from its value at  $\phi_{eq}$ .

113 LWA attains a large value whenever the deformation of Rossby wave is significant, thus  
114 blocking events can be identified by the detection algorithm similar to that in Liu and Wang  
115 (2024). In particular, when the LWA at a location exceeds a threshold relative to its climatology,  
116 a wave event can be identified and tracked by the longitude of peak LWA. We define the LWA  
117 threshold by first identifying the maximum observed value at each longitude, and then taking the

118 median of them. A blocking event is then defined when a wave event remain quasi-stationary  
119 (propagates less than of  $13.5^{\circ}$  in latitude and  $18^{\circ}$  in longitude per day), and persists for at least 5 days.

120

121 The return period is defined as the time difference between the onsets of consecutive blocking  
122 events within a given region. Figure 1 provides an example of the evolution of Z500 and LWA  
123 during two successive blocking events over the North Atlantic. The events are identified by the  
124 locations of maximum LWA, indicated by yellow crosses. The first event began on 29 June 1985  
125 (marked by the blue box) and persisted for 6 days. Twelve days after its onset, a second blocking  
126 event occurred in the same region on 11 July 1985. The distribution of such recurrence in blocking  
127 events thus characterizes the timescale over which the atmosphere returns to a blocked state in a  
128 given region. A strongly peaked recurrence distribution indicates that blocking events return with  
129 high regularity.

130 The LWA-based blocking climatology for summer (JJA) and winter (DJF) is shown in Figure 2.  
131 The main blocking regions over the Northern Pacific, Northern Atlantic, Greenland and Southern  
132 Pacific are clearly identified, consistent with patterns and frequency obtained using different  
133 blocking metrics (see a review from Woollings et al. (2018), Masato et al. (2013)). The latitudinal  
134 and longitudinal extent of the regions of focus in this study are listed in Table 1. We do not  
135 consider blocks over Greenland, as our red noise model is not well suited to capture the influence  
136 of topography on these blocks.

### 137 *c. Red Noise Models*

#### 138 1) AN ERA5-CONSTRAINED 2D MODEL

139 Inspired by the red noise model developed by Masato et al. (2009), we construct a similar two-  
140 dimensional (2D), i.e., longitude and time, red noise model, modified slightly to better fit the LWA

141 data. To be consistent with observed temporal and spatial coherence, the model is calibrated from  
 142 the daily LWA data at 50° N/S at 5° spatial resolution in longitude. The goal is to simulate the  
 143 anomalous LWA,  $\Delta W$ , as a function of longitude and time. It is built on the equations,

$$\Delta W_n^* = \phi \cdot \Delta W_{n-1} + \epsilon_n \quad (2)$$

$$\Delta W_n = \mathbf{A} \Delta W_n^*$$

144 where the vector  $\Delta W_n$  is the deviation of LWA from its climatological mean at each longitude at  
 145 a given time step  $n$ ,  $\phi$  is a longitude-dependent vector, the lag-1 temporal autocorrelation of each  
 146 longitude computed from the data, and  $\epsilon_n$  is a vector of white noise. The matrix  $A$  is empirically  
 147 derived to capture the observed spatial correlation pattern across longitudes, based on how each  
 148 point ( 5° of longitude) is correlated to its three neighboring points. It is therefore mostly zero  
 149 except for the 7 principal diagonals.

150 The details of model construction, as well as its temporal and spatial correlations, are provided  
 151 in Appendix A. Its statistics is a well match of the correlation patterns observed in ERA5.

152  
 153 Figure 3(a) shows the Hovmöller diagram of LWA in ERA5 data during 1985 JJA, the period of  
 154 Northern Atlantic blocking episodes shown in Figure 1. The onset of blocking events are marked  
 155 with crosses, and are also represented as a 1D time series to highlight their temporal distribution.  
 156 The same analysis from the ERA5-constrained 2D red noise model is presented in Figure 3(b),  
 157 where the LWA threshold for blocking has been adjusted to ensure the red noise model has the  
 158 same climatological frequency of events as observed. The red noise model accurately captures the  
 159 temporal and spatial coherence of the observation, particularly in terms of the duration and size of  
 160 wave events. With the absence of jet stream and Rossby wave dynamics in the red noise model,  
 161 however, “wave events” propagate both eastward and westward in a random fashion.

## 162 2) 1D AND 2D CONCEPTUAL MODELS

163 To investigate the roles of temporal and spatial parameters in shaping blocking recurrence  
164 patterns, a set of simplified red noise models are constructed. First, we consider a very simple, first  
165 auto-regressive (AR-1) model to describe the evolution of LWA in time only, governed by

$$\Delta W_n = \phi \cdot \Delta W_{n-1} + \epsilon_n \quad (3)$$

166 where  $\Delta W_n$  represents the deviation of LWA from its climatological mean at a single grid point  
167 and time step  $n$ ,  $\phi$  is the lag-1 temporal autocorrelation coefficient, and  $\epsilon_n$  is a white noise time  
168 series. The 1D model represents the simplest framework for describing the temporal pattern of  
169 blocking events. In this formulation, only the temporal correlation  $\phi$  and the total number of  
170 events, or onset frequency (set by the blocking threshold, or equivalently, amplitude of the noise),  
171 influence the distribution of blocks.

172  
173 A second 2D conceptual model shares the same equation 2 as the ERA5-constrained models,  
174 but with a simplified spatial correlation matrix  $A$ . The diagonals of matrix  $A$  are uniform across  
175 longitudes. This makes the variability statistically uniform in longitude, allowing us to explore the  
176 effect of domain size on the recurrence distribution.

## 177 3. Results

### 178 *a. Blocking recurrence statistics in reanalysis*

179 To investigate the structure of blocking recurrence, we analyze the LWA during blocking  
180 events and the probability distribution of the blocks preceding and proceeding a given event. The  
181 composites of LWA for all blocking events in JJA and DJF (with onset within the respective

182 season) are shown as red shading in the Hovmöller diagrams in Figure 4. The Hovmöller diagram  
183 is centered on the tracking longitude at onset (i.e., maximum point of LWA), and LWA is averaged  
184 over  $\pm 5^\circ$  in latitude relative to it. The resulting composites highlight the temporal and spatial  
185 characteristics of LWA during blocking events, exhibiting a pronounced peak at day 0, reflecting  
186 the stationarity and persistence of blocking.

187

188 To quantify where and when the preceding and proceeding blocking events occur, we com-  
189 posit the binary LWA masks of blocks occurring before and after each event, shown as purple  
190 shading. The fraction of times where the flow was previously/next blocked exhibits local maxima  
191 approximately 5–15 days before and after the reference event across all regions and in both seasons.

192 During boreal summer, pre- and proceeding blocks are more likely for Northern and Southern  
193 Pacific blocks compared to the Northern Atlantic blocks, reflecting the higher overall blocking  
194 frequency. Northern Pacific blocks have a more intense recurrence peaking at around 8-10 days,  
195 whereas the Southern Pacific blocks exhibit recurrence across a broader timescale, ranging from  
196 5-15 days. The recurrence signal is weaker in the Northern Atlantic over the range of 8-15 days,  
197 where synoptic variability dominates the high-latitudes. In contrast, the recurrence during winter  
198 for the Northern Pacific and Southern Pacific blocks is weaker and more dispersed compared to that  
199 in summer. Recurrence across longer timescale are observed, which break into several sub-peaks  
200 ranging from 5 to 17 days. This is consistent with the strong winter jet that advects wave activity  
201 eastward during winter. However, the recurrence for Northern Atlantic blocks becomes stronger  
202 during winter, peaking at a shorter timescale of 5-10 days, that is a defluent region where advection  
203 does not dominate.

204 Figures 5 and 6 show the return period distribution of blocks for ERA5 and the 2D red noise model  
205 in the Northern Pacific, Northern Atlantic, and Southern Pacific during boreal/austral summer and

206 winter. Return period is defined as number of days between the onsets of consecutive blocking  
207 events within the region. The corresponding Kernel density estimations (KDE) are plotted in the  
208 right panels (b), which attempt to reduce the sampling uncertainty. In the Northern Hemisphere,  
209 blocking events are more active in the Northern Pacific, where they persist longer and recur more  
210 frequently (see details of blocking durations and recurrence in Table 3). The peak of recurrence  
211 for the Northern Pacific blocks is more pronounced at 8.4 days. The Atlantic blocks return with a  
212 wider range with a peak at 11.4 days, while the Southern Pacific blocks exhibit a distinct peak of  
213 recurrence at 9.9 days. The enhanced recurrence peak in the Southern Pacific within sub-seasonal-  
214 to-seasonal frequency range may reflect the influence of the quasi-periodic annular mode (Liu and  
215 Wang 2023). The winter return period of blocks in the South Pacific shows a larger spread with a  
216 less distinct peak, consistent with the Hovmöller composite diagram in Figure 2. Both Northern  
217 Pacific and Northern Atlantic blocks have a shorter recurrence at 8.1 and 8.9 days, respectively.  
218 Recurrence at 11.9 days in the Southern Pacific appears weaker and more prolonged during winter.

219 The recurrence signal remains strong when using 4-day and 6-day blocking thresholds (results not  
220 shown), with the peak slightly shifting to 7–10 days and 10–18 days, respectively, due to changes in  
221 the total number of detected events. The dependence of the recurrence pattern on onset frequency  
222 and temporal correlation will be established in Session 3c. The choice of the 5-day threshold is  
223 consistent with the convention in the community, but modifying it does not change the physical  
224 insights of our results appreciably - affecting the return period distribution must exclusively by  
225 influencing the blocking rate.

### 226 *b. The blocking recurrence response to climate change*

227 Using the CESM1 model, we extend our blocking analysis to 1,799 years of data from the  
228 preindustrial control simulation and evaluate the blocking response to a warmer climate using 600

229 years of data from the RCP8.5 simulation. The spatial patterns of the observed blocking regions  
230 are well captured by this climate model.

231 Figure 7 shows the model bias from CESM1 preindustrial run simulation from (a) JJA and (b)  
232 DJF. Compared to ERA5, the rate of which the flow is blocked in CESM1 is higher in the Northern  
233 Pacific in both JJA and DJF, as well as in the Southern Pacific in JJA. Despite exhibiting an overall  
234 higher frequency of blocked states, CESM1 exhibits fewer blocking events because its events  
235 persist longer, see Table 3.

236 Figure 8 shows the response of the CESM1 block frequency in a warmer climate. The model  
237 projects a decrease in most blocking regions, with the exception of Greenland summer blocks  
238 and Pacific winter blocks over the Gulf of Alaska. In a warmer climate, the challenge posed  
239 by blocking-associated surface extremes lies less in changes in event frequency and more in the  
240 increased unpredictability of rare events. The implications of changes in blocking frequency for  
241 recurrence patterns are discussed further in a later section with insights drawn from the red noise  
242 model.

243 Figure 9 shows the return periods of blocking events from the CESM1 model, where the green  
244 and orange histograms represent results from the preindustrial control run and the RCP 8.5 run,  
245 respectively. To account for differences in sample size, the preindustrial simulation is subsampled  
246 into 600-year segments 100 times, and the results remain consistent and robust. The 8-12 day peak  
247 of recurrence can be observed among blocking events of CESM1.

248 To quantify differences in return-period distributions between the preindustrial and future cli-  
249 mates, we applied the Kolmogorov–Smirnov (KS) and Kullback-Leibler divergence test (KL div).  
250 The KS p-values are computed as the mean over 10,000 tests based on different subsamples of the  
251 data. As shown in Table 5, with the exception of Northern Pacific JJA blocks, the p-values exceed  
252 0.05 in all regions and seasons, indicating that there are no statistically significant differences in

253 the return-period distributions in a warmer climate. The frequency of onset in the Northern Pacific  
254 during JJA shows the largest decline, such that the null hypothesis of no change can be rejected.

255 *c. Conceptual understanding of blocking recurrence from red noise models*

256 1) RECURRENCE IN RED NOISE MODELS

257 Despite the mechanistic differences between observed blocking events and those generated by red  
258 noise, the recurrence of blocking can largely be explained by a red noise process (AR-1). Unlike  
259 Masato et al. (2009), who identified a distinct distribution pattern for the durations of blocks, we  
260 find that the return distribution of blocking is indistinguishable from an AR-1 process.

261 Table 4 lists the results of the statistical tests for the distributions of the return period in ERA5  
262 and the red noise model. As the sample sizes of ERA5 and the model are vastly different (82 vs  
263 20,000 years), the KS test has been repeated 10,000 times on sub-samples from the model. The  
264 p-values obtained are the mean across all tests. In addition, KL-div test has been carried out to  
265 quantify the differences between the KDEs from ERA5 and the model.

266 The return period distributions from ERA5 and the red noise model are statistically indistin-  
267 guishable for the Northern Pacific and Atlantic blocks from both seasons. The p-values are above  
268 the typical significance threshold, 0.05, indicating that the observations and the models likely come  
269 from the same distribution. In contrast, we can reject the null hypothesis that blocking recurrence  
270 in Southern Pacific in both seasons comes from the same distribution as the red noise model, with  
271 p-values lower than 0.05. With less zonal asymmetry in the Southern Hemisphere, blocking events  
272 in the Southern Pacific exhibit more temporal regularity, consistent with findings in Liu and Wang  
273 (2024) that blocking events in the region are enhanced by the quasi-periodic baroclinic annular  
274 mode. By and large, however, the red noise model captures the observed recurrence timescale and

275 overall distribution, offering conceptual insight into the processes that shape the temporal structure  
276 of blocking occurrence.

## 277 2) TEMPORAL FACTORS FROM 1D MODEL

278 In a 1D model where LWA evolves in time at a single grid point, the blocking return periods  
279 are determined by the model's temporal correlation and the onset frequency, defined by the total  
280 number of onsets over the number of days. Onset frequency is a convenient metric that can be  
281 measurable from observational data and is applicable to any blocking algorithm. The return period  
282 quantifies the temporal distribution of events, and the total number of onsets determines the mean  
283 spacing between successive events. To demonstrate the role of temporal parameters in blocking  
284 recurrence, we generate 200,000 years of data using 1D red noise models, with onset frequency,  
285  $\alpha = \text{Total number of onsets} / \text{Total number of days}$ , ranging from 1 to 9%, and temporal correlation  
286 coefficient from 0.1 to 0.8. Figure 10(a) shows the recurrence (i.e., the KDE peak of the return  
287 period distributions) across different onset frequencies, and the temporal correlation coefficients  
288 of 1D model runs. For an onset frequency below 2%, the peak of recurrence remains around 16  
289 to 18 days and varies little with temporal correlation. When probability of blocking is low, the  
290 return period distributions flatten (not shown) and skew towards the mean return period. Within the  
291 observed onset frequency range of 3-6%, the recurrence peaks show a stronger dependence on the  
292 temporal correlation, shifting toward a longer timescale as the temporal correlation increases. A  
293 stronger temporal correlation leads the model to persist in a given state for longer periods, thereby  
294 increasing the longevity of blocks and the time interval between blocking events. In particular,  
295 despite the simplicity of the 1D model, the observed 8–12-day recurrence time scale falls broadly  
296 within this onset-frequency regime.

297 Figure 10 also shows the return period distributions for (b) varying onset frequency with fixed  
298 temporal correlation of 0.7, and (c) varying temporal correlation with fixed onset frequency of  
299 5%. The values  $\phi = 0.7$  and  $\alpha = 5\%$  fall within the observed range from ERA5 (see details of  
300 observed  $\phi$  and  $\alpha$  in Table 4). Though the recurrence peaks remain largely within the 8-12 time  
301 window, the spreads and tails of the distributions vary substantially and are particularly sensitive to  
302 changes in onset frequency, where lower onset frequencies correspond to wider distributions. The  
303 dependence of distribution spread on onset frequency is also evident in the distribution of blocks in  
304 ERA5, as shown in Figures 5 and 6. Temporal correlation contributes to the spread and skewness  
305 of the distribution, with stronger temporal correlation corresponding to a wider and more centrally  
306 peaked distribution.

307 In the CESM1 simulations, the flattening of the return-period distribution for Northern Pacific  
308 JJA blocking in a warmer climate is associated with a nearly 1% reduction in onset frequency.  
309 Changes in temporal correlation or onset frequency smaller than 1% do not appear to produce  
310 statistically significant changes in the distribution.

### 311 3) THE IMPACT OF DOMAIN SIZE ON RECURRENCE

312 Using the zonally uniform 2D red noise models with varying domain sizes, we investigate the  
313 spatial factors that affect the return period distribution of blocking. Similar to the 2D model  
314 constructed for ERA5,  $\Delta W$  anomalies are spatially correlated to the neighboring three points  
315 (i.e.,  $15^\circ$ ), but with uniform spatial correlation coefficient across longitudes (matrix A in Eq. 2  
316 is uniform across longitudes). This modification is introduced for the convenience of varying  
317 the domain size. Note that our blocking detection algorithm does not impose any threshold on  
318 blocking size. Therefore, by varying the domain size in the model, we can examine both how  
319 recurrence changes with the size of blocking regions and how it depends on spatial coherence.

320 Results obtained from larger domain sizes can also be interpreted as representing domains with  
321 weaker spatial coherence and smaller blocking structures. The 2D models have been run for 20,000  
322 years, with domain sizes ranging from  $40^\circ$  to  $540^\circ$  in longitude. Values exceeding  $360^\circ$  should be  
323 interpreted as an increasing the planetary radius which fixing the deformation radius (see domain  
324 size details in the legend of Figure 12).

325 Figures 11 (a) and (b) show the recurrence peak and onset frequency of the 2D models in varying  
326 domain sizes and temporal correlations. Recall from Figure 10 that the recurrence peak is inversely  
327 related to the onset frequency of the domain. Although the spatial distribution of blocks varies  
328 with domain sizes, the return period depends only on the temporal spacing between blocks, and  
329 is therefore largely controlled by the number of onsets within the domain. In other words, the  
330 general behavior of recurrence can be inferred from the climatological blocking frequency of a  
331 given domain, regardless of its spatial coherence or size.

332 The observed blocking basins in ERA5 correspond to a domain size of  $60^\circ$  longitude and temporal  
333 correlations in the range of  $\phi = 0.5 - 0.7$ , yielding recurrence peaks of approximately 5 to 10 days.  
334 This is close to the observed 8-12-day window, despite the simplified spatial coherence structure in  
335 the models. The upper right part of Figure 11(a) exhibits recurrence peaks of 1 day, indicative of an  
336 exponential-like distribution. Larger domain sizes favor such a distribution, such that for domain  
337 exceeding  $180^\circ$  (not shown), the distribution becomes exponential-like, peaking at 1 day regardless  
338 of temporal correlation. This reflects the increased blocking frequency in the lesser domain.

339 Figure 12 shows the onset frequency per degree of longitude for domain sizes ranging from  $40^\circ$   
340 to  $540^\circ$ . The onset frequency increases proportionally with domain size when the domain expands  
341 from  $40^\circ$  to  $80^\circ$ , as shown by the nearly constant values in the plot. A rapid increase in onset  
342 frequency appears between  $80^\circ$  and  $100^\circ$ . This increase in blocking probability arises when the

343 domain becomes large enough to allow an additional blocking episode to occur simultaneously.  
344 Such transition also occurs between 36 and 48 grid points, and again between 360° and 420°.

345 The transition effect of the domain size is also evident in the return-period distributions (at  
346  $\phi = 0.7$ ) shown in Figure 13(a). At domain sizes of 40° to 80°, the distributions vary little and  
347 remain similar to AR-1 like distributions. As the domain size increases, the distribution changes  
348 drastically from 100° onward, becoming a rapidly decaying function with a peak at 1 day. This  
349 distribution resembles that of a 2D white noise model, as shown in Figure 13(b). Although the red  
350 noise model prescribes spatial correlation among neighboring points, each subsection of the domain  
351 remains spatially coherent internally, but is not effectively correlated with other subsections. With  
352 increasing domain size, the temporal pattern of blocking onsets is no longer dominated by the  
353 red-noise-like behavior of individual subsections, but instead by the collective pattern arising from  
354 all subsections, which operate independently.

#### 355 **4. Conclusions**

356 Understanding the regularity of the temporal features of the blocks can help us to better predict the  
357 blocks. Using ERA5 reanalysis data and a climate model output, we find a preferential recurrence  
358 of blocks on the timescale of 8-12 days robustly across regions and seasons. We find, however, that  
359 the recurrence, or return period distribution, can be qualitatively reproduced by a simple AR(1)  
360 red-noise model. The AR(1) model shows how the recurrence distribution depends critically on  
361 the temporal correlation of synoptic variability and the rate of block onset.

362 An increase in the blocking frequency, for instance, associated with enhanced atmospheric vari-  
363 ability over a given region or in response to a climate perturbation, decreases the peak recurrence  
364 timescale. The mean separation between blocks is inversely related to the rate. Increased per-  
365 sistence of the flow is associated with opposing effects: increasing the likelihood of an extended

366 blocking event, but also slowing the variation of the flow. On balance, increased persistence flattens  
367 the recurrence spectrum, tending to increase the peak recurrence period. This finding prompts us  
368 to re-think the dynamics of atmospheric blocking. That the recurrence distribution can be closely  
369 matched by an extremely simple AR(1) process suggests that blocking can be viewed as the tail end  
370 of the red spectrum of synoptic variability. Variations in the amplitude of synoptic variability (the  
371 local wave activity) still matter, as do their temporal decorrelation, as these factors set the overall  
372 blocking frequency. In future work, it would be interesting to investigate whether this recurrence  
373 can be better explained by the quasi-periodic behavior inherent in an AR(2) process – implying  
374 the importance of memory blocking dynamics — but it would likely require a very long climate  
375 integration to definitively rule out a simple red noise null hypothesis.

376 These findings enable us to interpret the recurrence in climate models integrations of past and  
377 future climates. CESM1’s preindustrial control and and RCP 8.5 simulations exhibit consistent  
378 recurrence period distributions, suggesting no major changes in the temporal structure of blocking  
379 in response to global warming. In a warmer climate, however, the blocking frequency generally  
380 declines, leading to a broader return period distribution. While this leads to a subtle decrease in  
381 the overall risk of weather extremes associated with blocking, the return distribution will broaden  
382 out, potentially making them more challenging to forecast.

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385 *Data availability statement.* The ERA5 reanalysis is available at <https://www.ecmwf.int/en/forecasts/datasets/reanalysis-datasets/era5>. The authors acknowledge the use of  
386 outputs from the CESM large-ensemble (LENS) project.  
387

## ERA5-constrained Red Noise Model

The 2D red noise model constructed extends the framework from Masato et al. (2009) to capture the observed temporal and spatial correlation of LWA from ERA5. The model is constructed at daily resolution with 5° longitude spacing. Following Equation 2,  $\Delta W$  denotes the deviation of LWA from its seasonal mean,  $\phi$  is the observed lag-1 autocorrelation, a function of longitude, and  $\epsilon$  is a Gaussian white noise term, which also varies in longitude to match the observed variance.

The spatial correlation matrix  $A$  is defined and optimized in the following way: the matrix is partitioned into six longitudinal segments to represent large-scale spatial heterogeneity. The elements of  $A$  are parameterized using correlation strength, decay rate, and asymmetry. The optimal parameters are obtained by minimizing the combined error in temporal autocorrelation and zonal spatial correlation between the model and ERA5. The optimization is performed using a bounded L-BFGS-B algorithm with multiple initializations.

Figure 14 shows the temporal and spatial correlations of ERA5 (solid lines) and the ERA5-constrained 2D red noise model (dotted lines) in the Northern and Southern Hemispheres during (a–b) JJA and (c–d) DJF. Consistent with the model validation in Masato et al. (2009), the correlations produced by our red noise model qualitatively resemble those observed in ERA5.

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TABLE 1. Blocking regions in ERA5

<b>Region</b>	<b>Season</b>	<b>Longitude Range</b>	<b>Latitude Range</b>
Northern Pacific	JJA	150°E–150°W	50°–70°N
Northern Pacific	DJF	120°E–180°E	45°–65°N
Northern Atlantic	JJA	60°W–0°	55°–75°N
Northern Atlantic	DJF	30°W–30°E	40°–60°N
Southern Pacific	DJF	170°E–130°W	70°–50°S
Southern Pacific	JJA	120°W–60°W	70°–50°S

TABLE 2. Blocking regions in CESM1 simulations

<b>Region</b>	<b>Season</b>	<b>Longitude Range</b>	<b>Latitude Range</b>
Northern Pacific	JJA	150°E–150°W	55°–75°N
Northern Pacific	DJF	120°E–180°E	45°–65°N
Northern Atlantic	JJA	60°W–0°	55°–75°N
Northern Atlantic	DJF	30°W–30°E	40°–60°N
Southern Pacific	DJF	170°E–130°W	65°–45°S
Southern Pacific	JJA	130°W–70°W	70°–50°S

TABLE 3. Blocking statistics in ERA5 and CESM1 model simulations

Region	Season	Recurrence (day)			Duration (day)		
		ERA5	CTRL	RCP 8.5	ERA5	CTRL	RCP 8.5
Northern Pacific	JJA	8.4	9.3 *	10.4	8.2	8.3	8.1
Northern Atlantic	JJA	11.4	9.7	9.6	7.5	7.4	8.0
Southern Pacific	DJF	9.9	7.4	8.3	7.9	7.7	7.1
Northern Pacific	DJF	8.1	7.6	7.5	7.4	7.8	7.5
Northern Atlantic	DJF	8.9	7.8	8.1	8.2	8.1	7.8
Southern Pacific	JJA	11.9	8.9	8.8	7.1	7.5	7.4

TABLE 4. Statistics for return period distributions in ERA5 and red noise model

<b>Region</b>	<b>Season</b>	$\phi$	<b>Onset freq, ERA5 (%)</b>	<b>Onset freq, model (%)</b>	<b>p-value (mean)</b>	<b>KL-div</b>
Northern Pacific	JJA	0.71	5.12	5.14	0.130	0.041
Northern Atlantic	JJA	0.66	4.37	4.44	0.221	0.050
Southern Pacific	DJF	0.66	4.30	4.35	0.005	0.029
Northern Pacific	DJF	0.63	5.39	5.37	0.050	0.075
Northern Atlantic	DJF	0.78	4.06	3.91	0.112	0.050
Southern Pacific	JJA	0.61	3.08	3.03	0.016	0.069

TABLE 5. Statistics for return period distributions in CESM1 simulations

<b>Region</b>	<b>Season</b>	$\phi$ , CTRL	$\phi$ , RCP 8.5	Onset freq, CTRL (%)	Onset freq, RCP 8.5 (%)	p-value (mean)	KL-div
Northern Pacific	JJA	0.79	0.82	4.09	3.10	0.01	0.019
Northern Atlantic	JJA	0.72	0.72	3.32	3.45	0.42	0.006
Southern Pacific	DJF	0.67	0.65	3.32	2.63	0.18	0.011
Northern Pacific	DJF	0.76	0.76	4.24	3.69	0.34	0.009
Northern Atlantic	DJF	0.83	0.81	3.04	2.78	0.22	0.012
Southern Pacific	JJA	0.73	0.68	3.51	3.53	0.30	0.004

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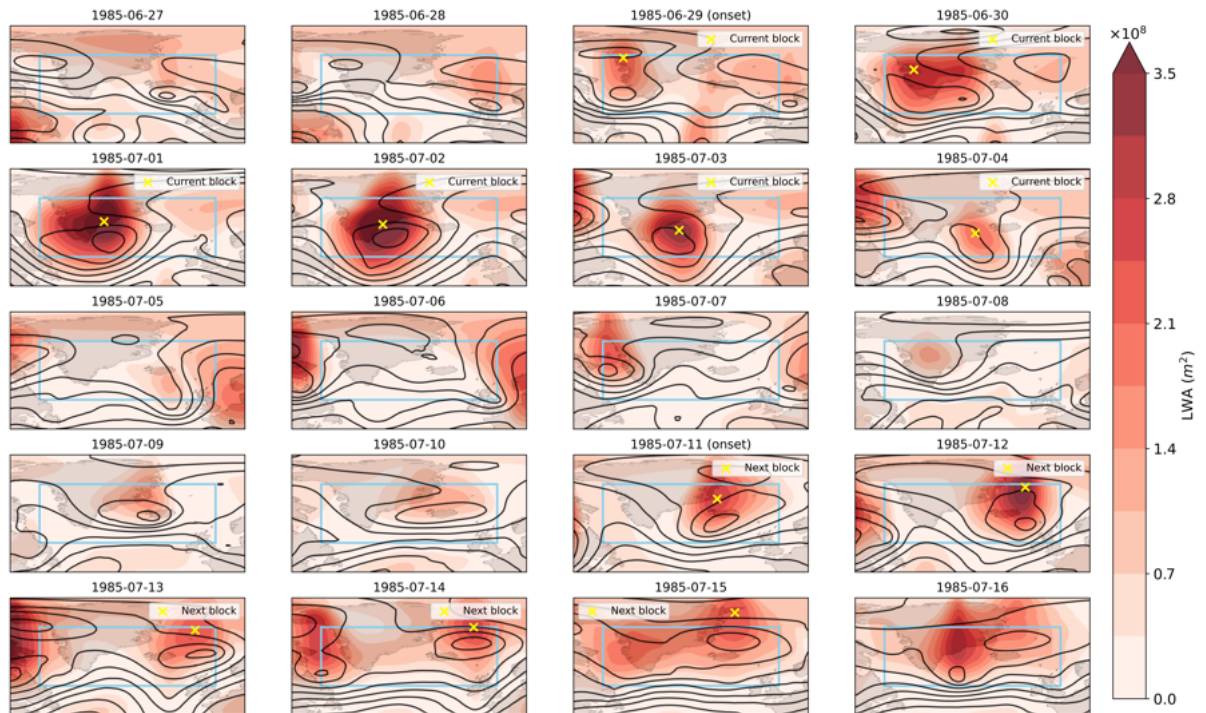
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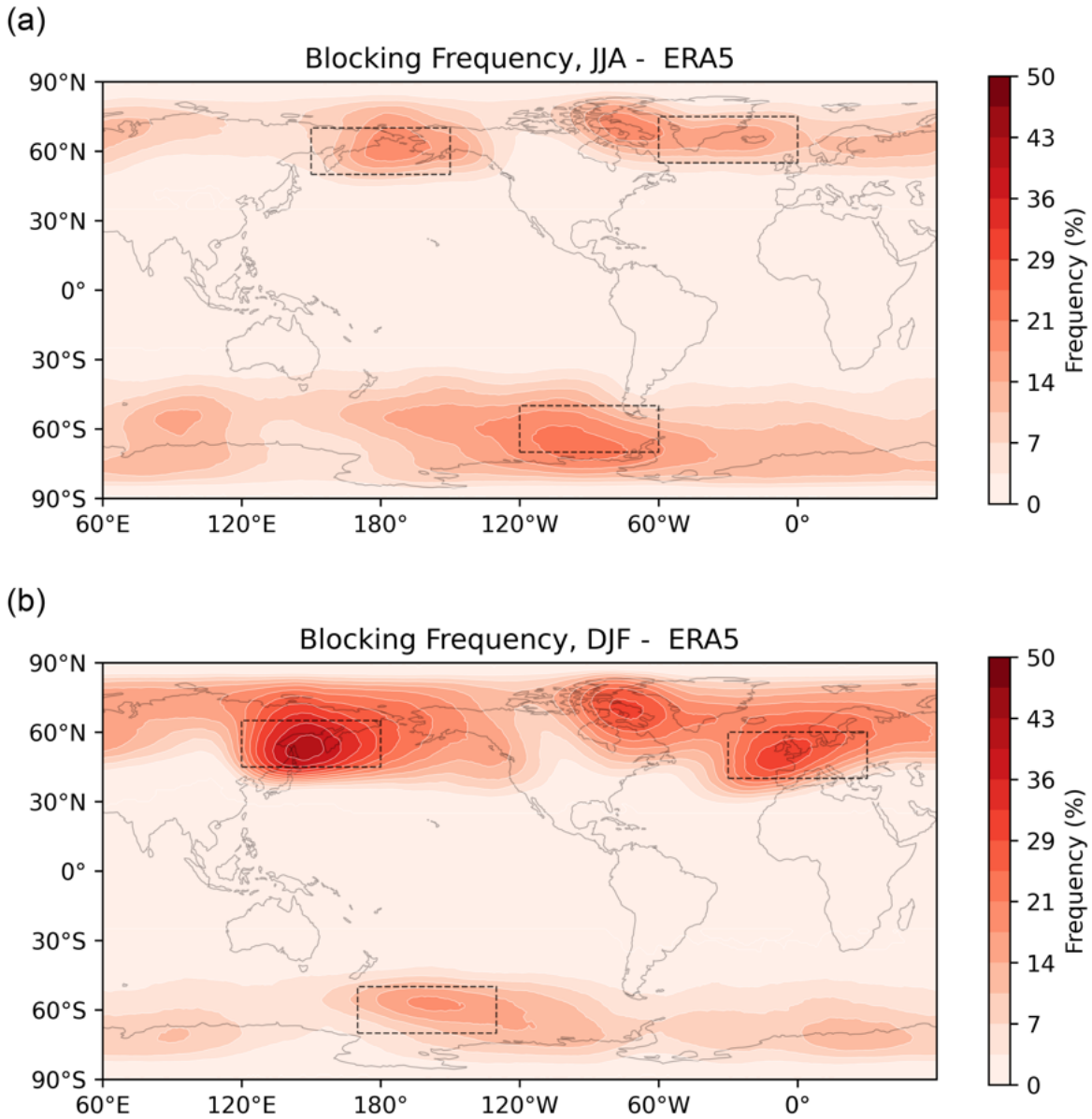
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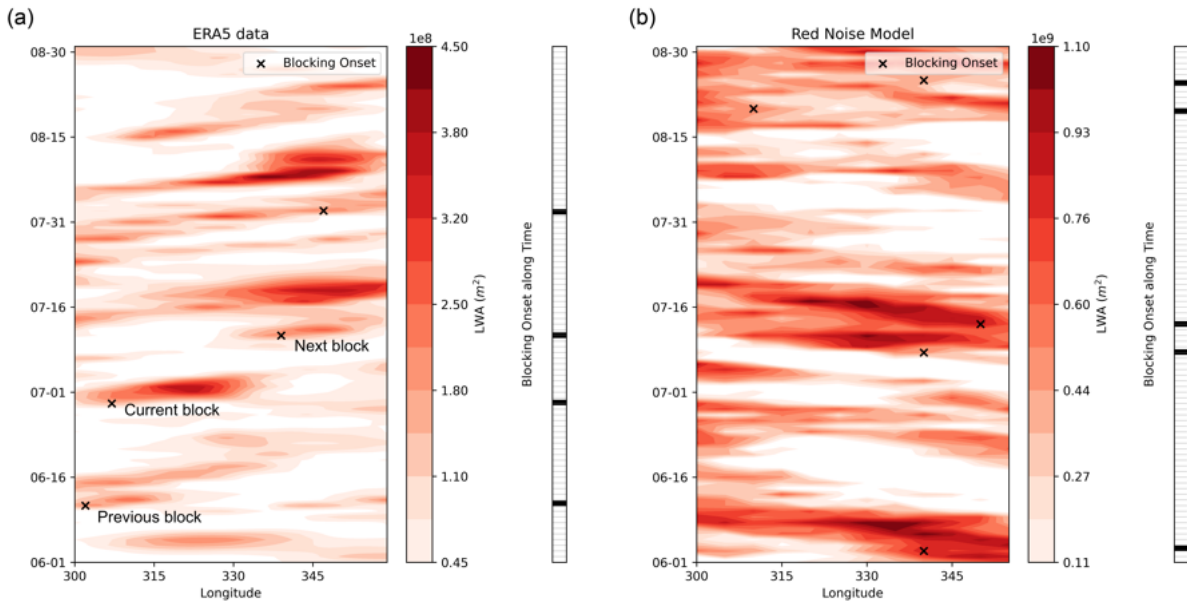
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593	red noise model (dotted) in both hemispheres during (a-b) JJA and (c-d) DJF . . . . .	47



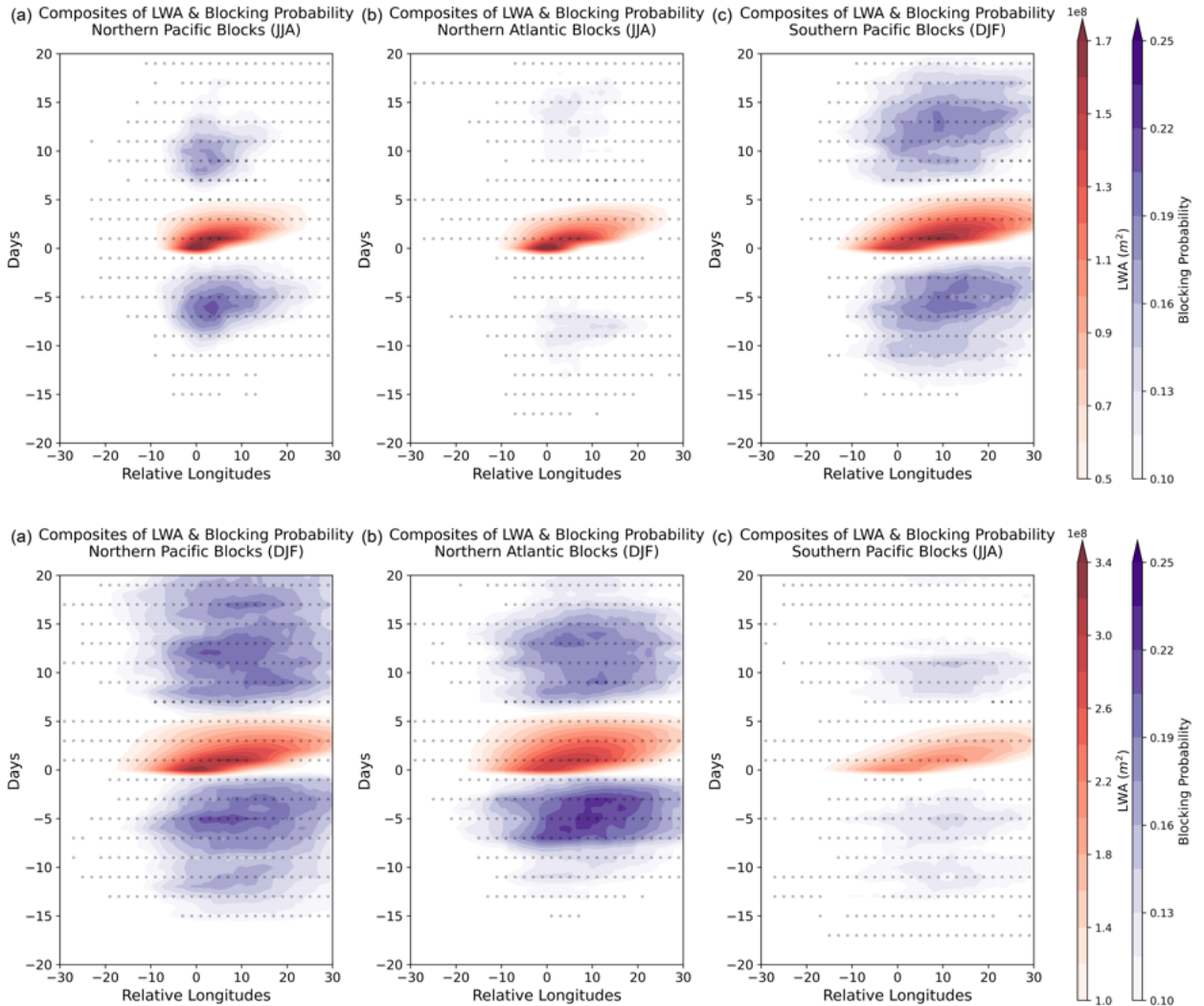
594 FIG. 1. Z500 contour plots with LWA shading showing a recurring blocking episode over the Northern Atlantic  
 595 on 29 June 1985 and 11 July 1985. Event tracking points are marked by yellow crosses, and the region used for  
 596 the return period calculation is indicated by the blue box. Z500 contours range from 5000 to 5975 m at 75 m  
 597 intervals



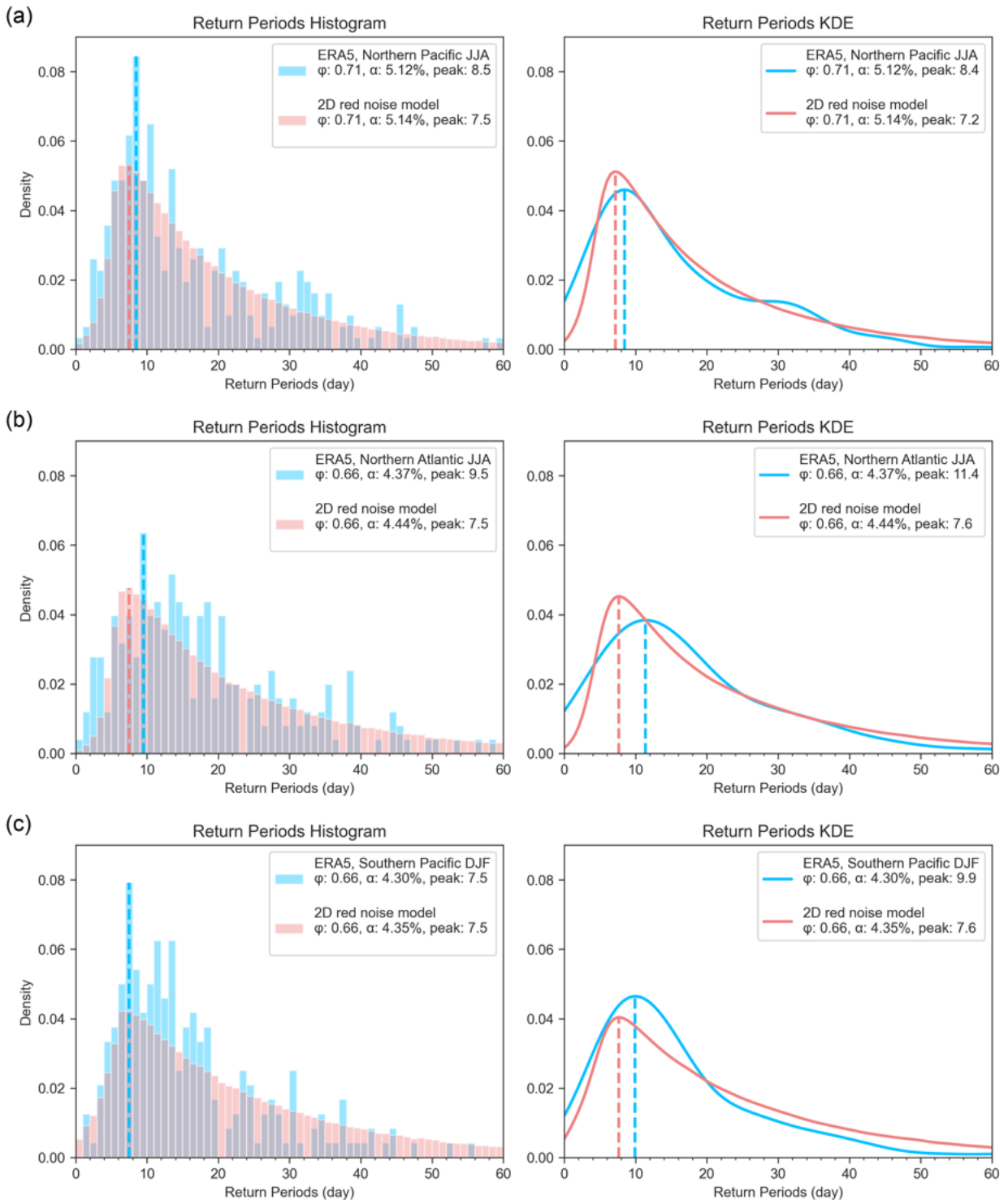
598 FIG. 2. The percentage of time the flow is blocked, as a function of latitude and longitude, in ERA5 reanalysis  
 599 over the period 1940–2022 for (a) JJA and (b) DJF. Regions used for recurrence analysis in ERA5 are indicated  
 600 by boxes.



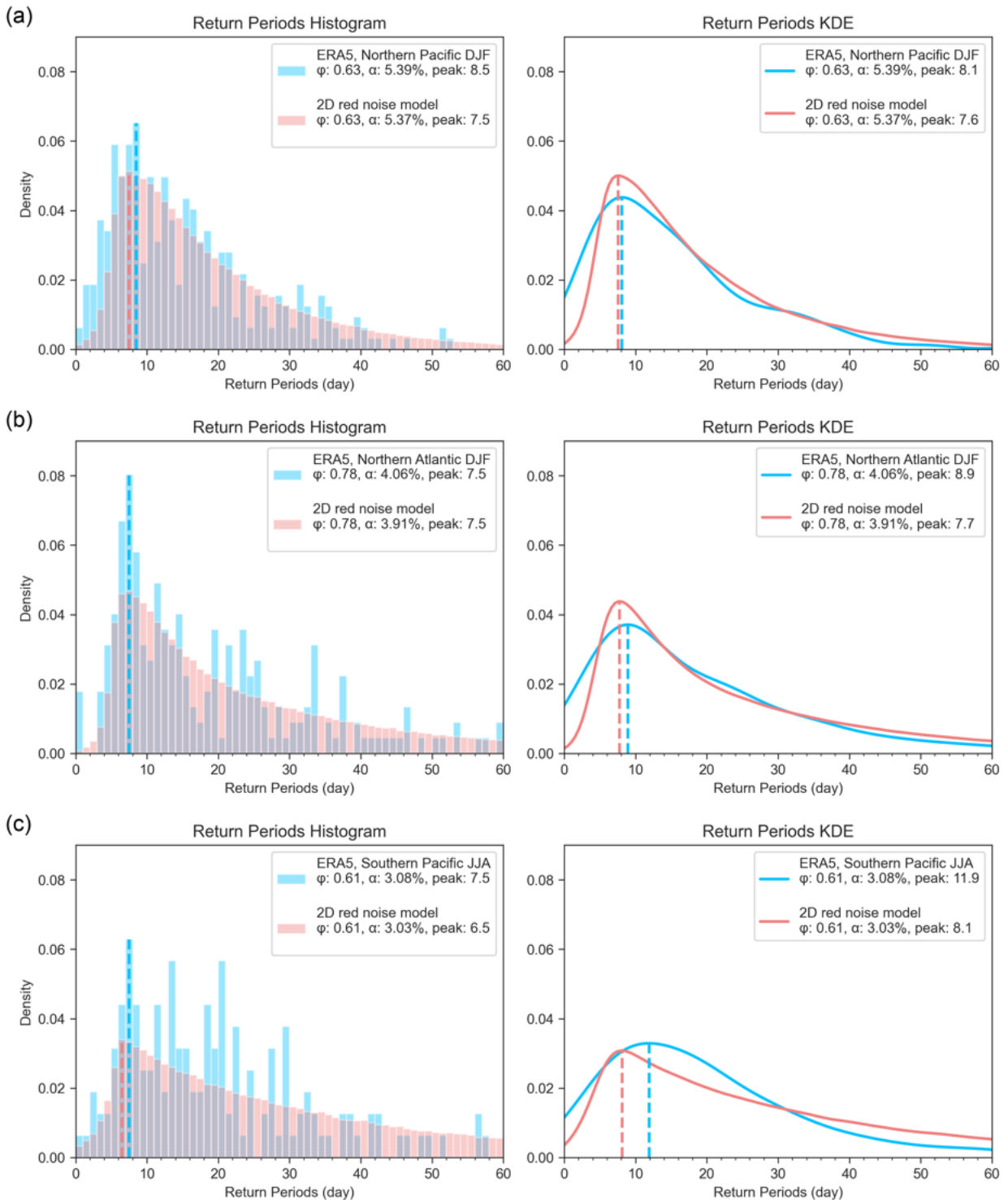
601 FIG. 3. Hovmöller diagram of LWA from (a) ERA5 in 1985 JJA and (b) the red noise model for the Northern  
 602 Atlantic region (150°E-150°W). The LWA from ERA5 has been averaged over latitudes 55°-77°N. Blocking  
 603 onsets are marked by crosses, between which the return period is defined. They are also indicated on the 1D  
 604 timeline array to the right of each diagram.



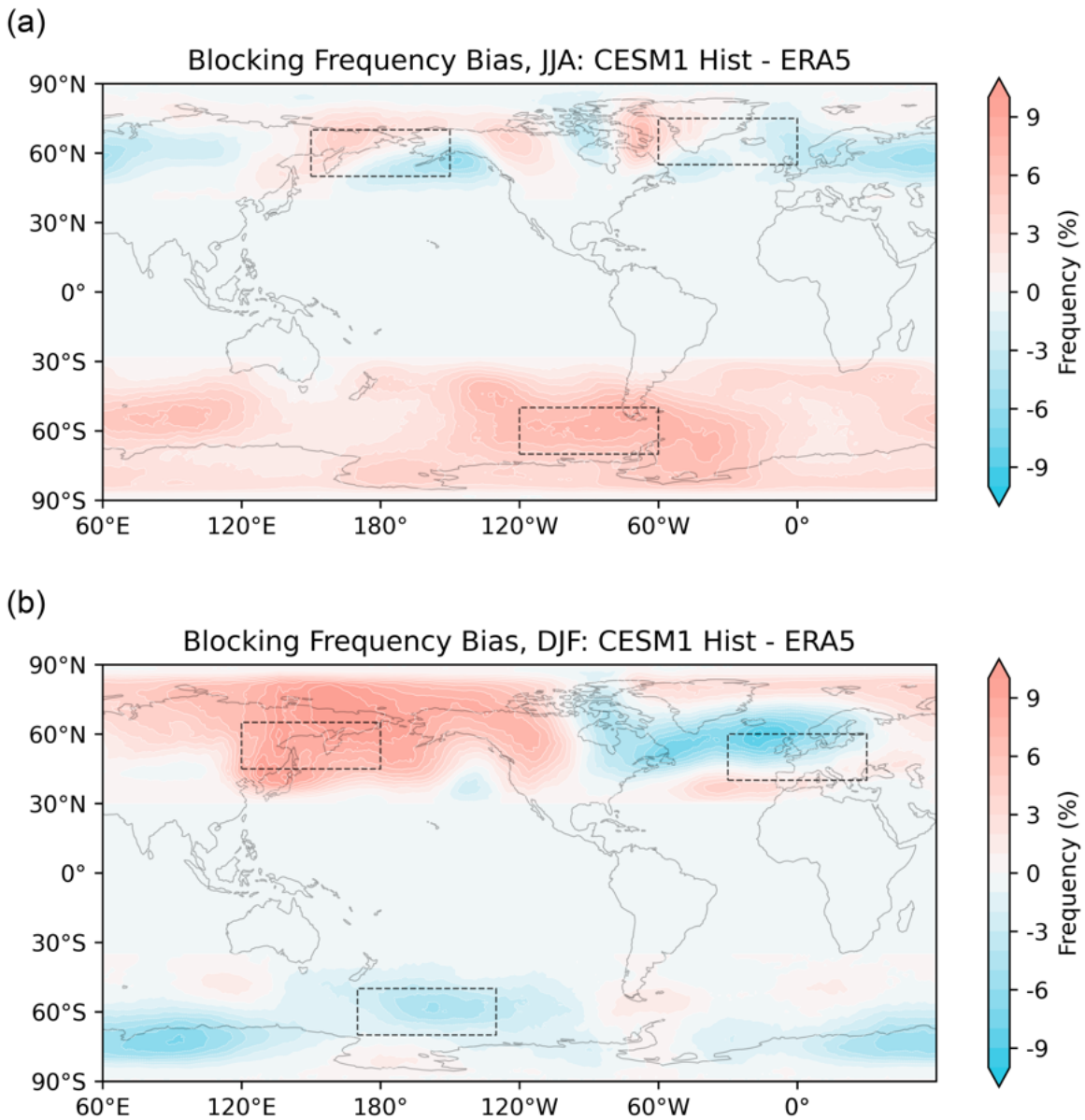
605 FIG. 4. Composites of LWA from ERA5 in the Northern Pacific (left), Northern Atlantic (middle), and  
 606 Southern Pacific (right) for boreal/austral summer (a–c) and winter (d–f). Red shading shows LWA associated  
 607 with blocking events, centered on the onset day and aligned by the longitude of the reference tracking point,  
 608 with values averaged over  $\pm 5^\circ$  latitude. Purple shading indicates the fraction of time there was a preceding and  
 609 subsequent blocking events at the location and lead/lag time. Black dots denote grid points significant at the 0.99  
 610 level.



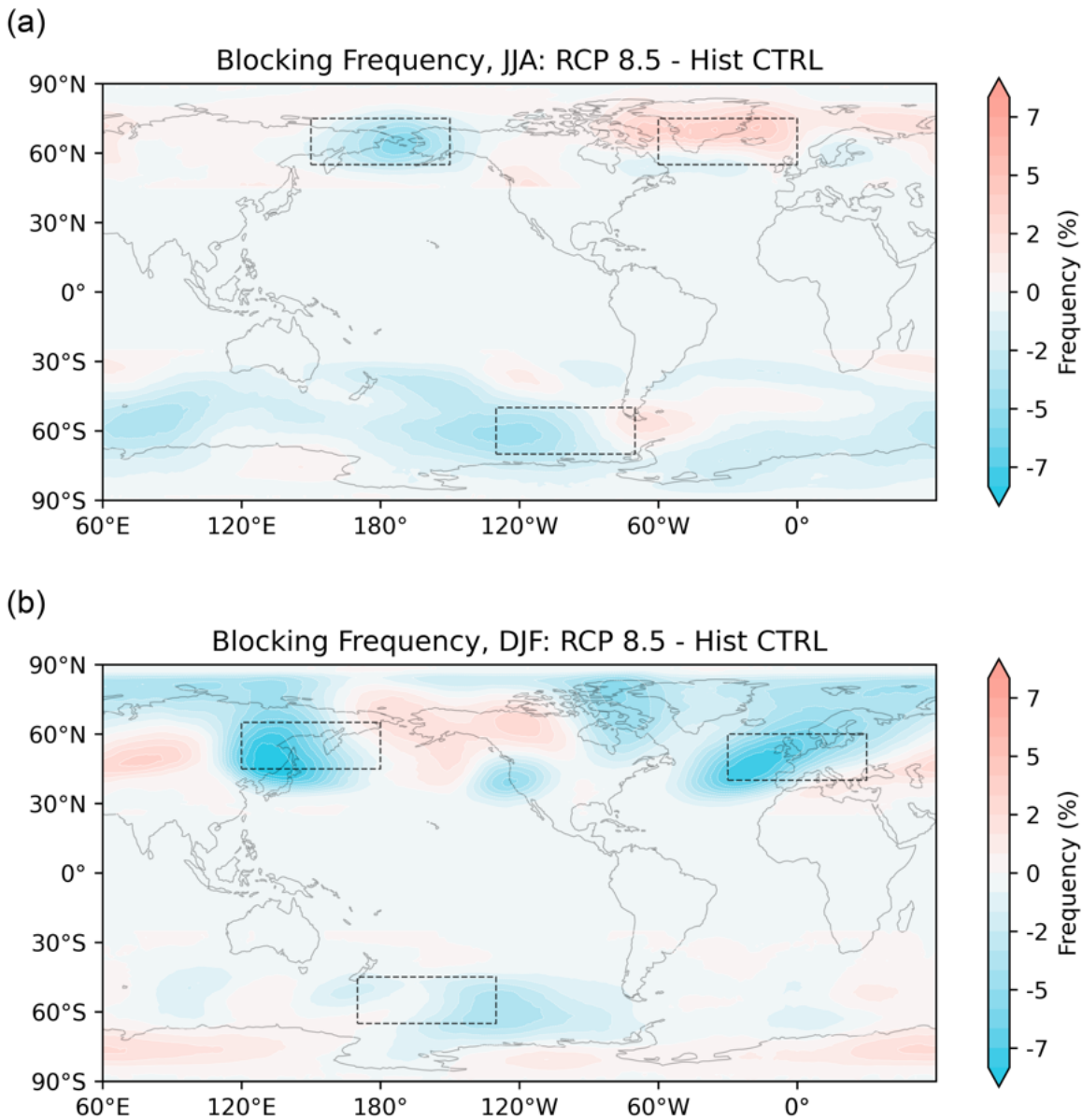
611 FIG. 5. Histograms and corresponding KDE plots of return periods from ERA5 (blue) and corresponding  
 612 ERA5-constrained 2D red noise model (red) during summertime for (a) Northern Pacific, (b) Northern Atlantic  
 613 and (c) Southern Pacific regions. Dashed lines mark the peaks of the histograms and KDE curves, indicating the  
 614 recurrence timescale



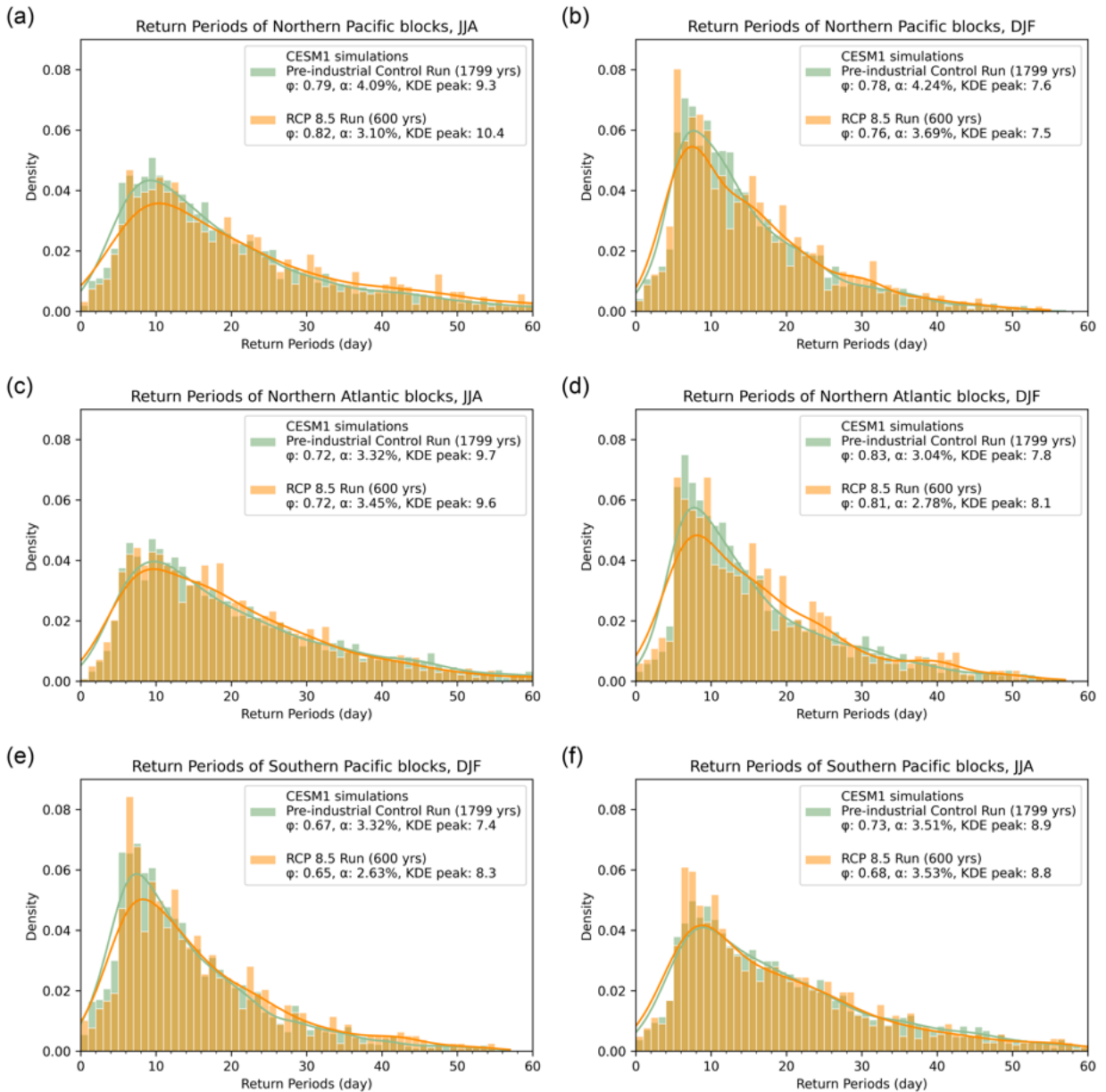
615 FIG. 6. Histograms and corresponding KDE plots of return periods from ERA5 (blue) and corresponding  
 616 ERA5-constrained 2D red noise model (red) during wintertime for (a) Northern Pacific, (b) Northern Atlantic,  
 617 and (c) Southern Pacific regions. Dashed lines mark the peaks of the histograms and KDE curves, indicating the  
 618 recurrence timescale



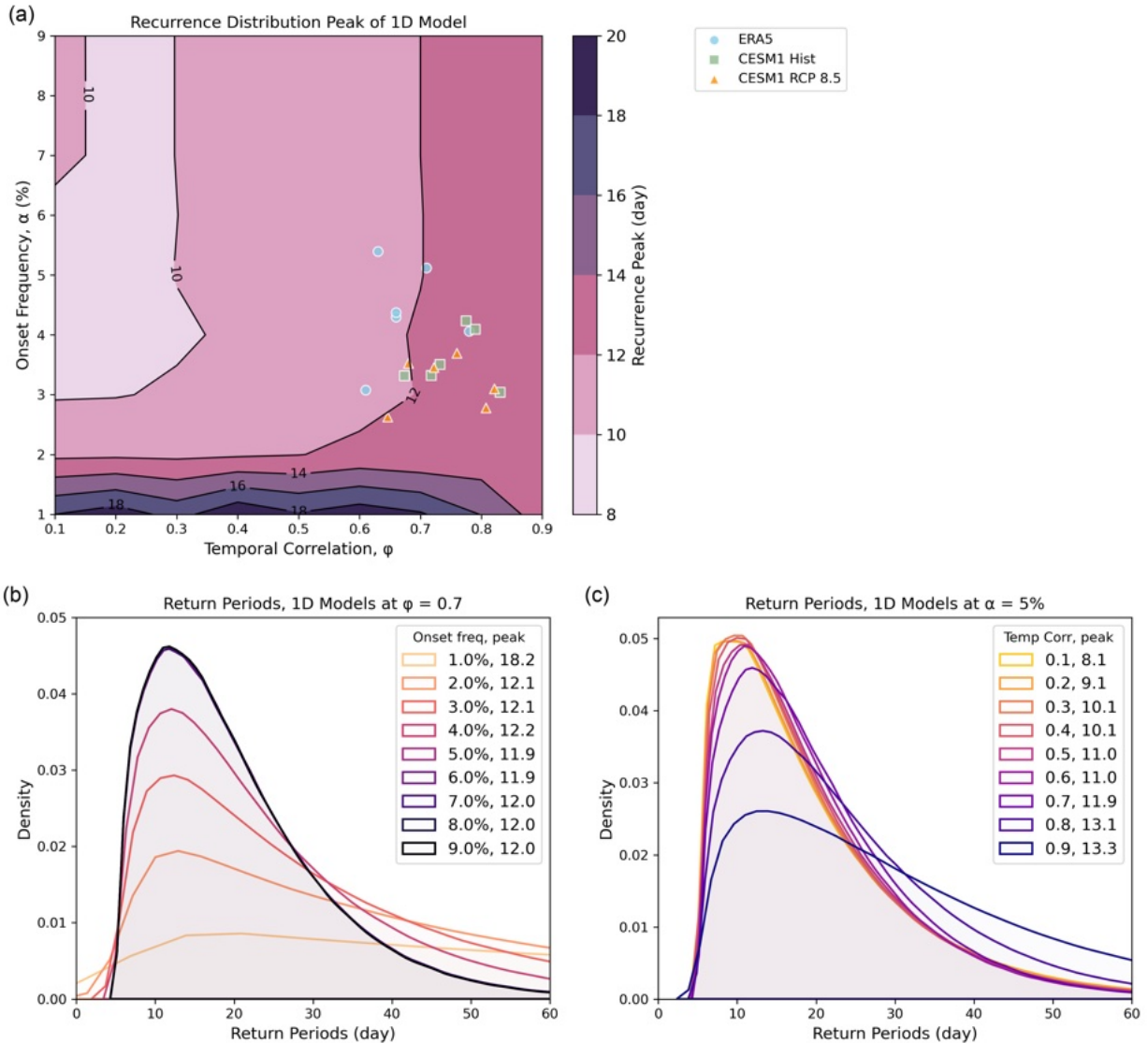
619 FIG. 7. Blocking frequency bias from CESM1 Hist CTRL simulation for (a) JJA and (b) DJF. Regions used  
 620 for recurrence analysis in ERA5 are indicated by boxes.



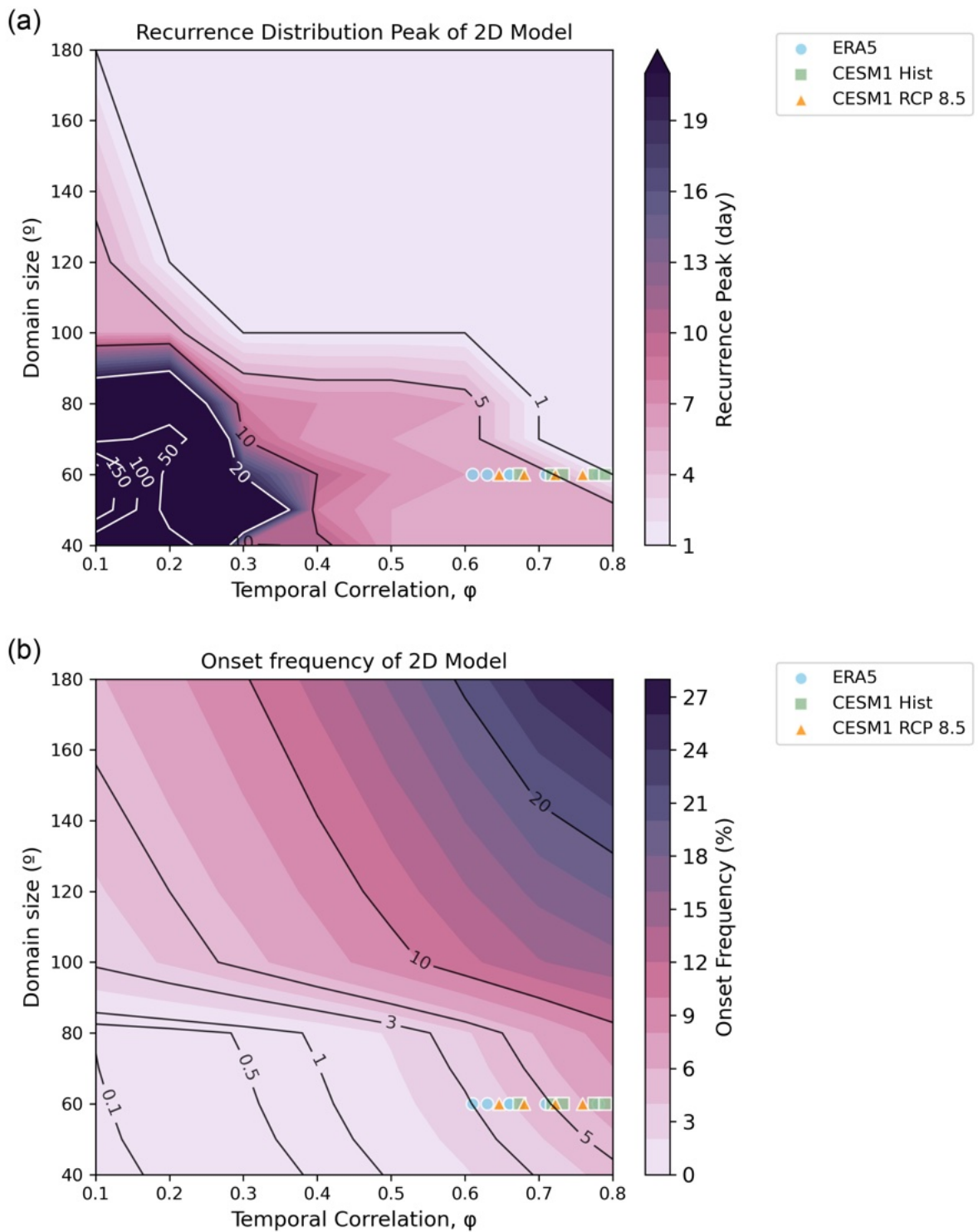
621 FIG. 8. Blocking frequency response from CESM1 simulations for (a) JJA and (b) DJF. Regions used for  
 622 recurrence analysis in CESM1 are indicated by boxes.



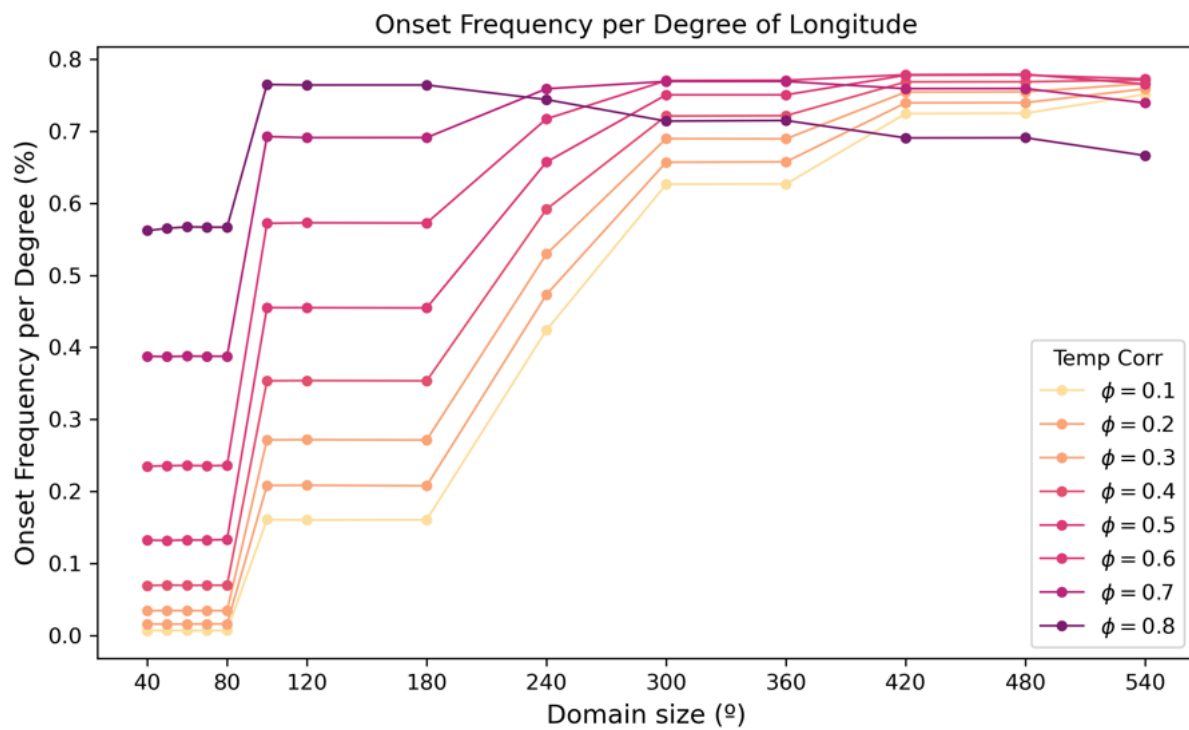
623 FIG. 9. Histograms and corresponding KDE curves of return periods from CESM1 model for preindustrial  
 624 control simulation (green) and RCP 8.5 simulation (orange) during summer and wintertime for (a-b) Northern  
 625 Pacific, (c-d) Northern Atlantic, and (e-f) Southern Pacific regions



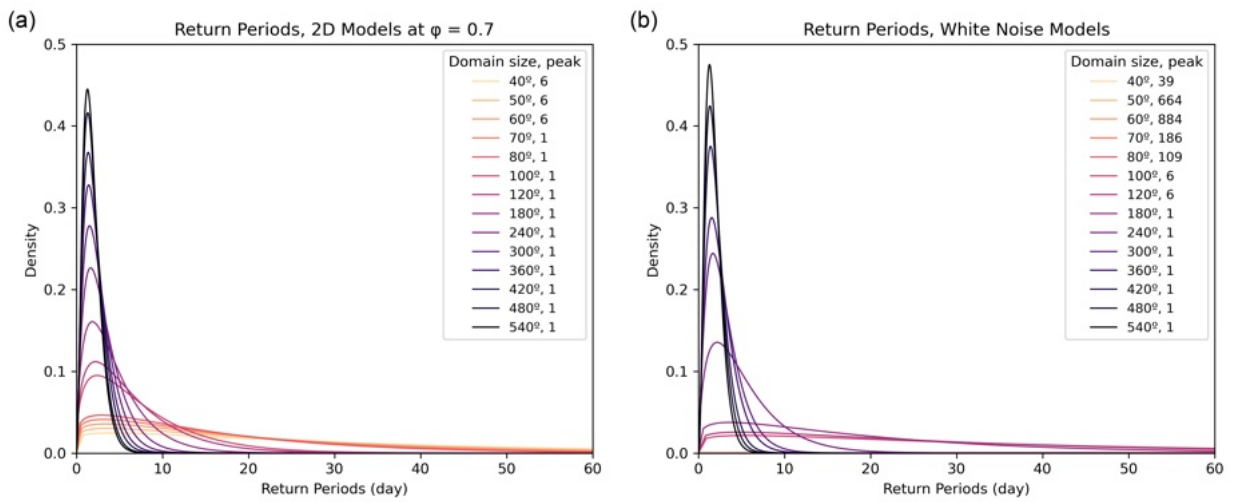
626 FIG. 10. (a) Table of recurrence peaks for the 1D conceptual red noise models across temporal correlations  
 627 and onset frequency, with markers indicating temporal correlation coefficients and onset frequencies from ERA5  
 628 (blue circle), CESM pre-industrial run (green square) and RCP 8.5 run (orange triangle), (b) return period  
 629 distributions across onset frequencies at temporal correlation,  $\phi = 0.7$ , and (c) return period distributions across  
 630 temporal correlations at onset frequency,  $\alpha = 5\%$  for the 1D red noise models



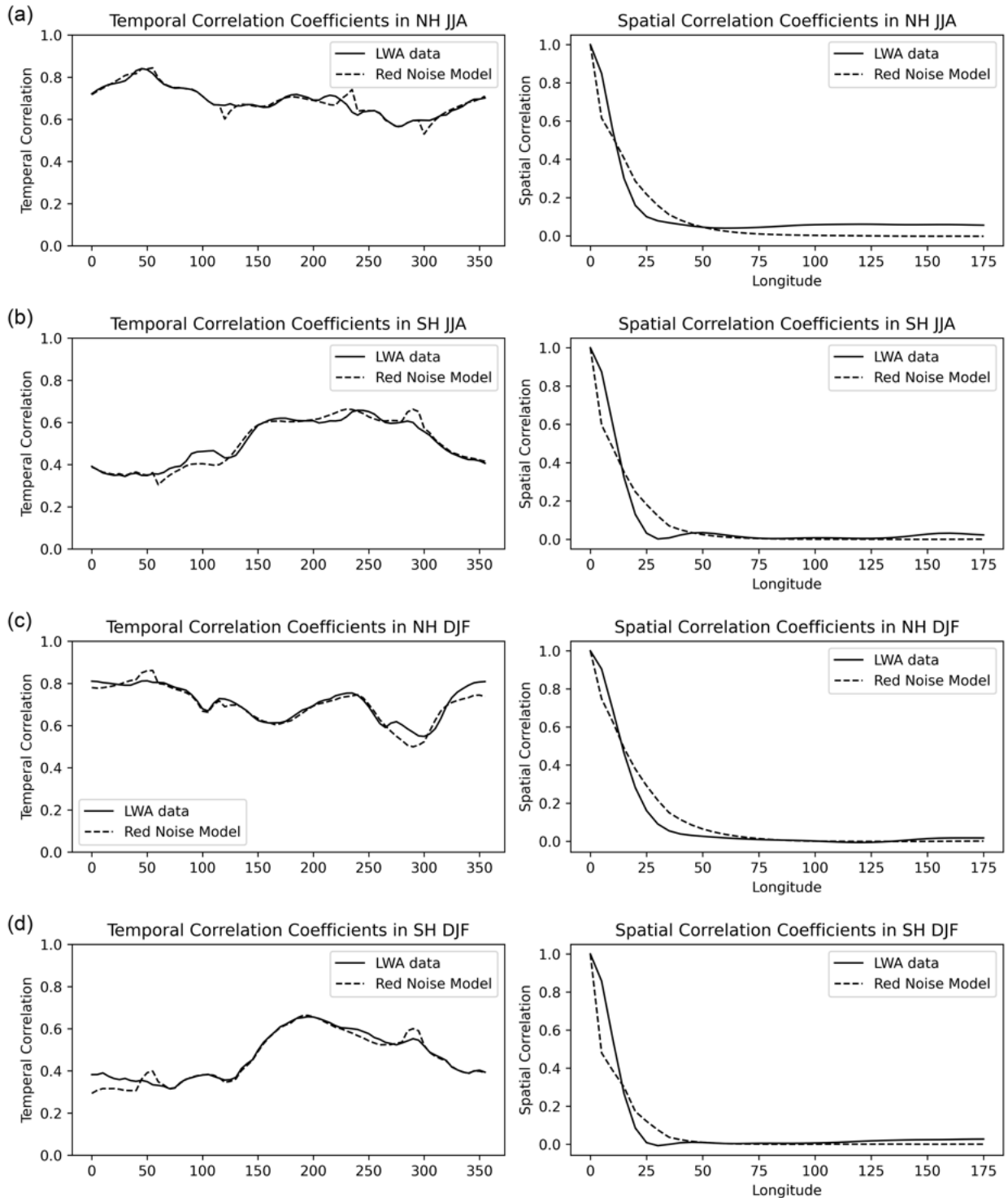
631 FIG. 11. (a) Table of recurrence peaks and (b) onset frequency for the 2D conceptual red noise models across  
 632 temporal correlations and domain sizes, with markers indicating temporal correlation coefficients and domain  
 633 size from ERA5 (blue circle), CESM pre-industrial run (green square) and RCP 8.5 run (orange triangle)



634 FIG. 12. Onset frequency per degree in longitude across domain sizes at different temporal correlations in the  
 635 2D red noise conceptual models



636 FIG. 13. (a) Return period distributions (with gamma fitting) in the 2D conceptual red noise models across  
 637 domain sizes at temporal correlation,  $\phi = 0.7$ , and (b) return period distributions (with gamma fitting) in 2D  
 638 white noise models across domain sizes



639 FIG. 14. Temporal and spatial correlations of LWA in ERA5 (solid) and the ERA5-constrained 2D red noise  
 640 model (dotted) in both hemispheres during (a-b) JJA and (c-d) DJF