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3 Supporting Information for

4 **Uncertainty in the response of sudden stratospheric warmings and stratosphere-**
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34 **Contents of this file**

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36 Figure S1

37 Tables S1 to S5

38 **Introduction**

39 We include one figure and five tables in this supporting information.

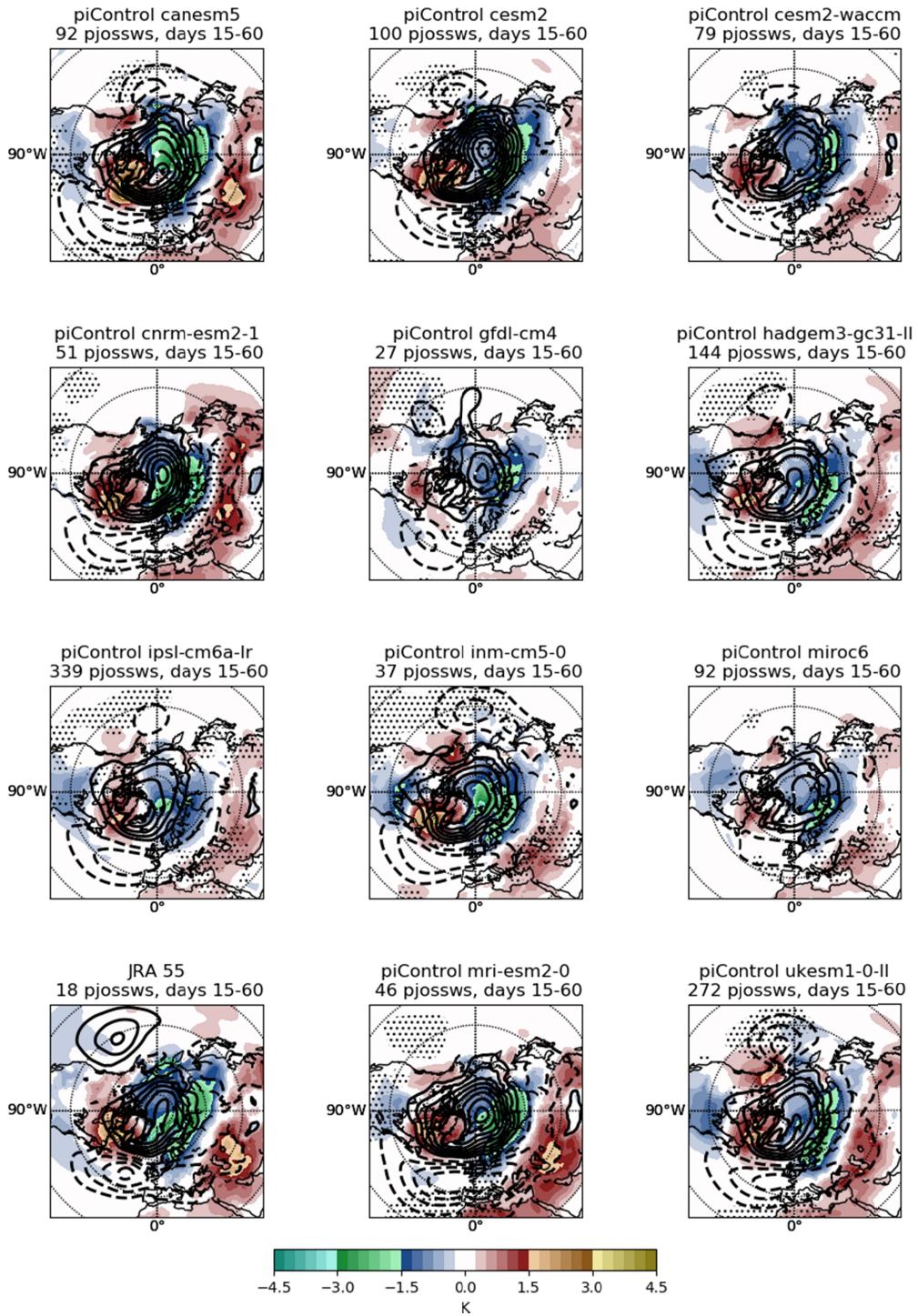
40 Figure S1 shows the composite maps of anomalous SLP (contours) and 2m temperature
41 (shading) after Polar Night-Jet Oscillation (PJO) events averaged over 15/60 days after central
42 date in piControl simulation and JRA-55 simulation (bottom left). Stippling indicates stat.
43 significant differences from JRA-55 reanalysis at the 95% confidence level. Comparing this
44 figure with Figure 7 of the manuscript, we confirm that the tropospheric response to PJOs is
45 stronger than for all sudden stratospheric warmings (SSWs).

46 Table S1 displays the annual frequency of SSW events in the historical simulations (1958-2014
47 period) in each model and serves as model validation for simulating SSW events in the
48 historical period. These values are also shown in Figure 1a.

49 Tables S2 displays information about changes in frequency of SSWs under high CO₂ loading
50 conditions. More specifically, it shows the annual frequency of SSW events in the piControl
51 and abrupt4xCO₂ simulations along with the difference of these frequencies and the statistical
52 information about its significance. Figure 1b is built with this information.

53 Table S3 shows the standard deviation of daily zonal-mean zonal wind at 10hPa and 60°N (m s⁻¹)
54 in the piControl and abrupt4xCO₂ simulations.

55 Table S4 and S5 present information about the trend estimates of SSW frequency and the time
56 of emergence of this trend. Table S4 is complementary to Figure 5a and Table S5 contains the
57 values shown in Figure 5b.



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63 **Figure S1.** Composite maps of anomalous SLP (contour interval: 1 hPa) and 2m temperature
64 (shading, K) after PJOs (averaged over 15/60 days after central date) in the piControl
65 simulation and JRA-55 reanalysis (bottom left). Stippling indicates stat. significant differences
66 from JRA-55 reanalysis at the 95% confidence level.

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model	Freq. historical	Difference	p-value (parametric test)	p-value (bootstrapping test)
GFDL-CM4	0.30	-0.33	0.0087	0.0046
CESM2	0.30	-0.33	0.0087	0.0039
CanESM5	0.36	-0.28	0.033	0.020
UKESM1-0-LL	0.48	-0.16	0.27	0.20
INM-CM5-0	0.54	-0.10	0.48	0.37
MIROC6	0.55	-0.09	0.56	0.43
CESM2-WACCM	0.59	-0.05	0.74	0.65
MRI-ESM2-0	0.62	-0.01	0.93	0.85
CNRM-ESM2-1	0.66	0.02	0.88	0.91
HadGEM3-GC31-LL	0.73	0.09	0.54	0.52
IPSL-CM6A-LR	1.00	0.36	0.032	0.0098

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66 **Table S1.** Annual frequency of SSW (events per winter) in the historical simulations (period:
 67 1958-2014). The values of the historical frequency are compared with the estimate from the
 68 JRA-55 re-analysis (0.64 SSW winter⁻¹). Values in bold indicate that the model SSW frequency is
 69 statistically significantly different from JRA-55 one at a 95% confidence level

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model	Freq. piControl	Freq. abrupt 4xCO ₂	Difference	p-value (parametric test)	p-value (bootstrapping test)
HadGEM3-GC31-LL	0.75	0.32	-0.44	8x10⁻¹¹	<1 x10⁻⁴
CanESM5	0.45	0.13	-0.32	9.3x10⁻¹¹	<1 x10⁻⁴
IPSL-CM6A-LR	0.76	0.49	-0.27	3.3x10⁻¹⁵	<1 x10⁻⁴
INM-CM5-0	0.50	0.34	-0.16	0.034	0.0231
GISS-E2-2-G	0.25	0.14	-0.11	0.16	0.14
UKESM1-0-LL	0.54	0.48	-0.063	0.33	0.29
GFDL-CM4	0.32	0.38	0.059	0.4	0.31
MRI-ESM2-0	0.48	0.56	0.078	0.32	0.25
CESM2	0.23	0.37	0.14	0.0031	8 x10⁻⁴
CNRM-ESM2-1	0.53	0.69	0.16	0.026	0.007
MIROC6	0.46	0.67	0.21	0.0019	<1 x10⁻⁴
CESM2-WACCM	0.46	0.80	0.34	2.8x10⁻⁶	<1 x10⁻⁴

71 **Table S2.** Annual frequency of SSW (events per winter) in the piControl and abrupt4xCO₂
 72 simulations along with the difference of these frequencies. Values in bold indicate that the
 73 abrupt4xCO₂ value is statistically significantly different from the piControl one at a 95%
 74 confidence level

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model	std. piControl [m s ⁻¹]	std. abrupt 4xCO ₂ [m s ⁻¹]	Difference [m s ⁻¹]
HadGEM3-GC31-LL	17.0	16.5	-0.5
CanESM5	13.9	11.9	-2.0
IPSL-CM6A-LR	14.6	16.9	2.3
UKESM1-0-LL	16.9	17.7	0.6
GFDL-CM4	11.6	12.3	0.7
MRI-ESM2-0	16.3	17.4	1.1
CESM2	15.3	17.0	1.7
CNRM-ESM2-1	17.1	18.6	1.7
CESM2-WACCM	11.7	12.3	0.6
MIROC6	14.2	15.8	1.6
GISS-E2-2-G	17.1	15.9	-1.2
INM-CM5-0	15.7	15.5	-0.2

79 **Table S3.** Standard deviation of daily zonal-mean zonal wind at 10hPa and 60°N (m s⁻¹) in the
 80 piControl and abrupt4xCO₂ simulations. Difference values in bold indicate statistically
 81 significant values at a 95% confidence level (Pearson values).

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Model	Trend	p-value
CanESM5	0.96	0.036
HadGEM3-GC31-LL	0.96	0.0045
IPSL-CM6A-LR	0.99	0.27
INM-CM5-0	0.99	0.81
UKESM1-0-LL	1.00	0.94
CESM2	1.02	0.57
MIROC6	1.03	0.14
CNRM-ESM2-1	1.03	0.023
CESM2-WACCM	1.05	0.034
GFDL-CM4	1.05	0.048
MRI-ESM2-0	1.08	0.0011

84 **Table S4.** Trend estimates of SSWs for the 1pctCO₂ runs. The trend is expressed in terms of the
 85 fractional change in SSW frequency per decade.

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Model	Trend	Decade of Emergence
MRI-ESM2-0	1.08	4
CESM2-WACCM	1.05	8
GFDL-CM4	1.05	9
HadGEM3-GC31-LL	0.96	11
CNRM-ESM2-1	1.03	11
CanESM5	0.96	14

93 **Table S5.** Decade of emergence of the trend of SSWs for models where the trend is significant
 94 based on Table S4.